

Information theory meets human-computer interaction

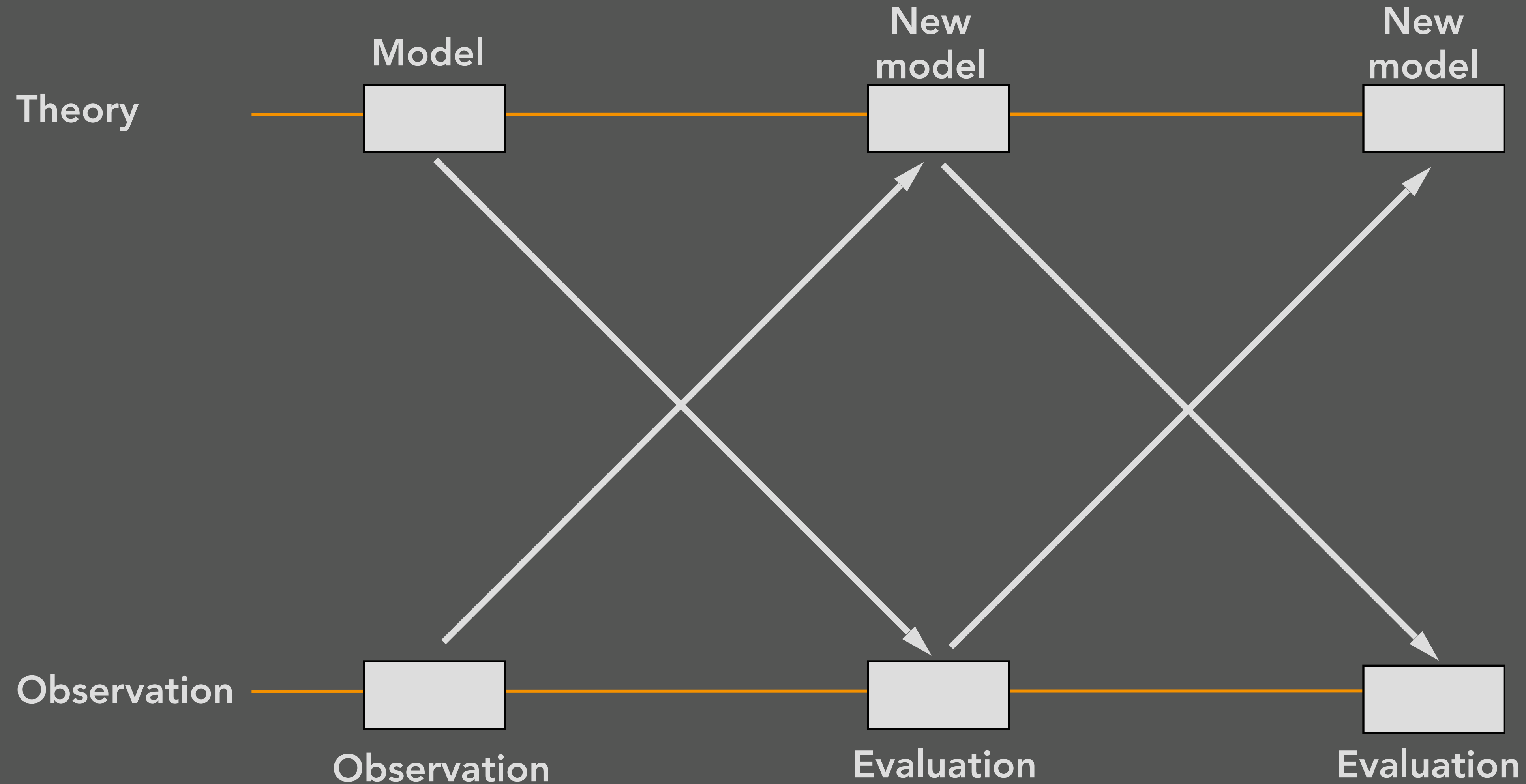
Michel Beaudouin-Lafon
Université Paris-Saclay

SystemX
15 mars 2023

Theory in Human-Computer Interaction

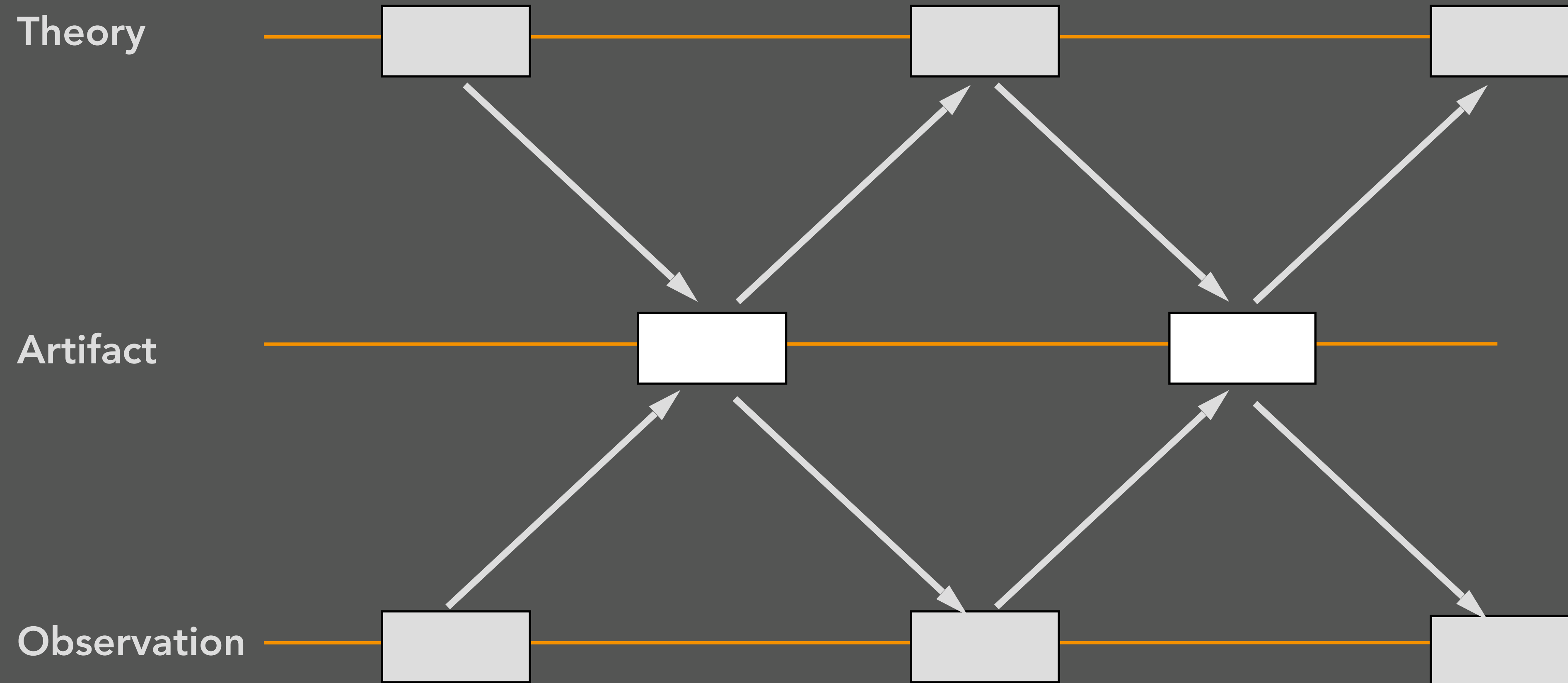
Theory in Natural Sciences

Mackay & Fayard, 1997



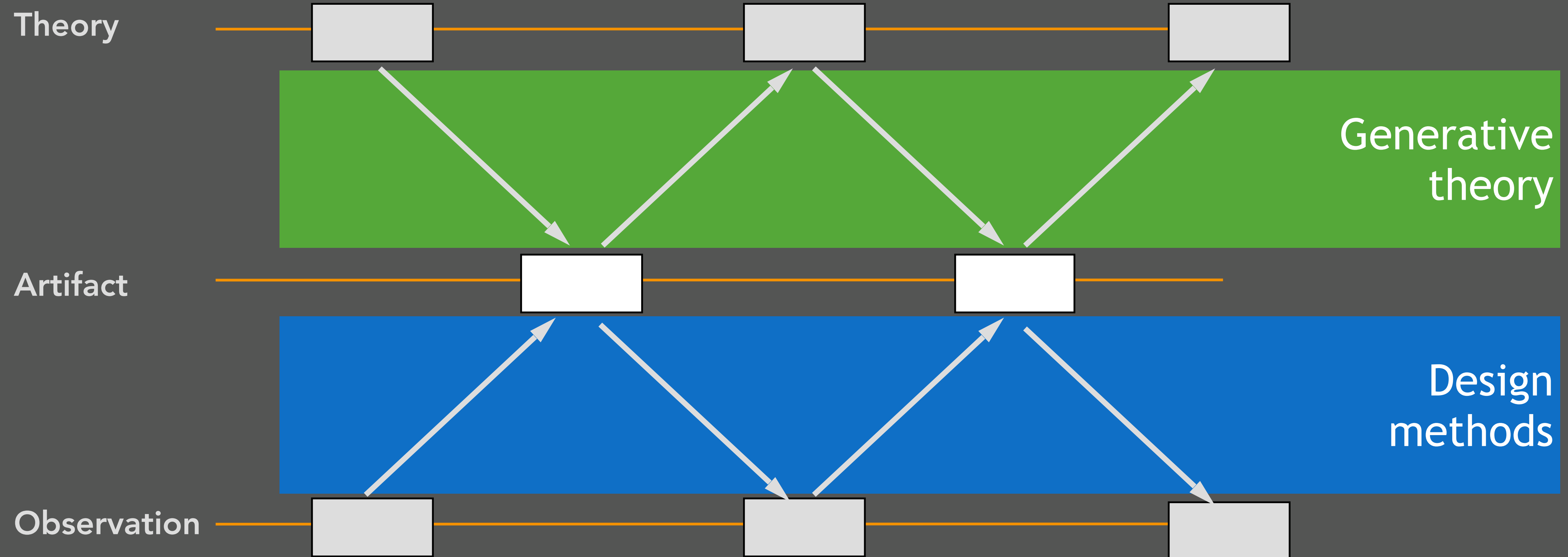
Theory and HCI

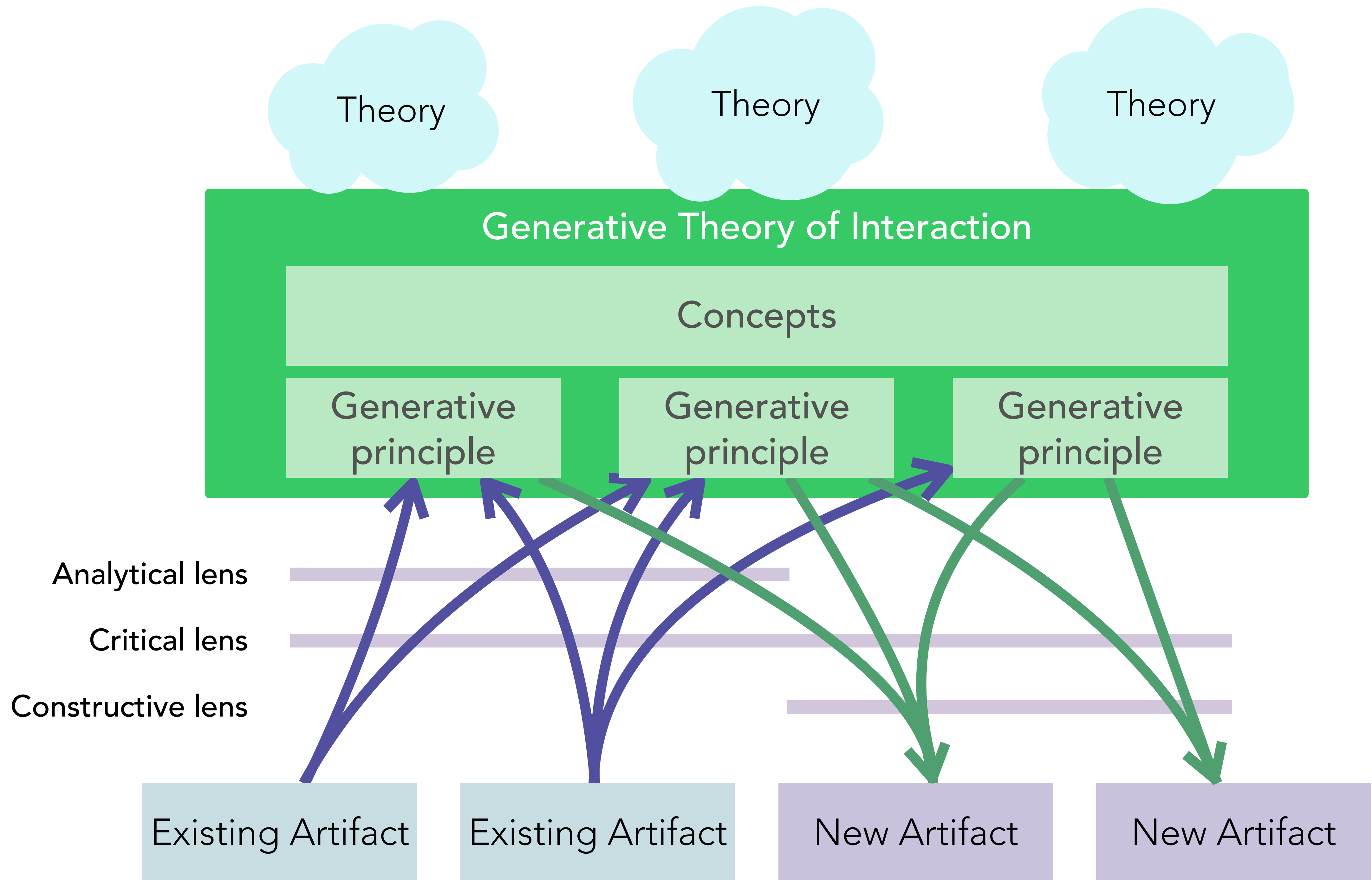
Mackay & Fayard, 1997



Theory and HCI

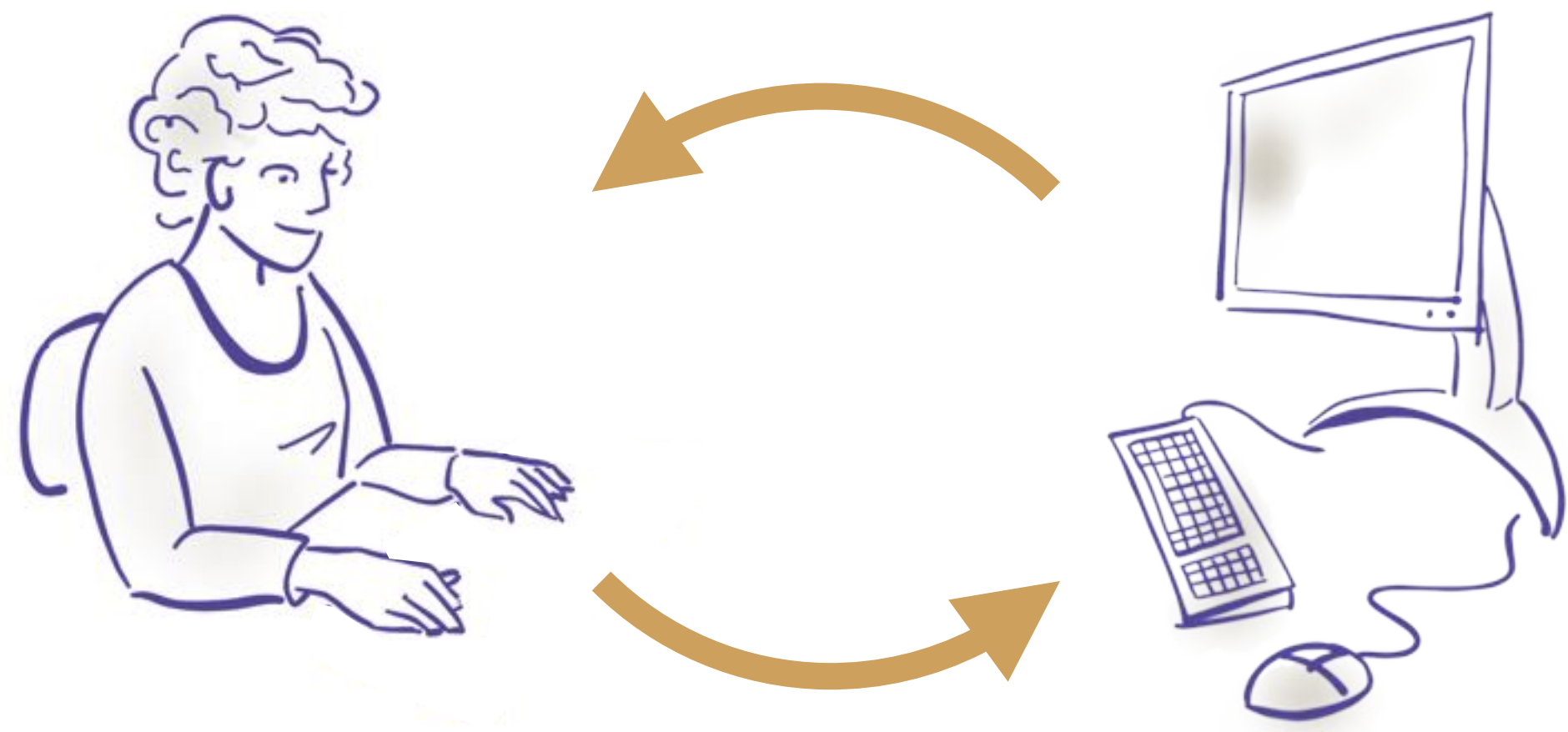
Beaudouin-Lafon, Bødker & Mackay, 2021





Information

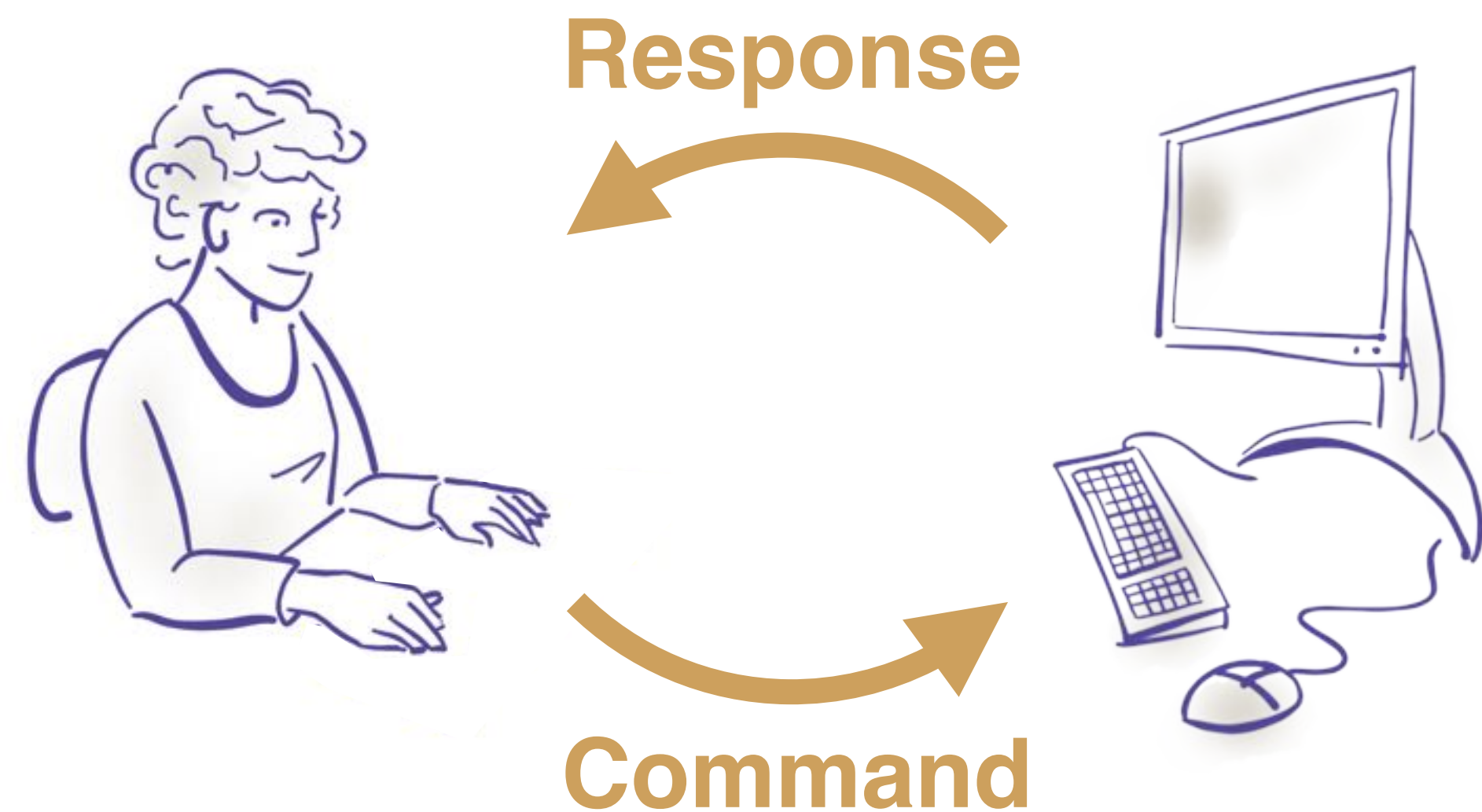
Interaction as a phenomenon



What is sent by the user
to the computer?

What is sent by the computer
to the user?

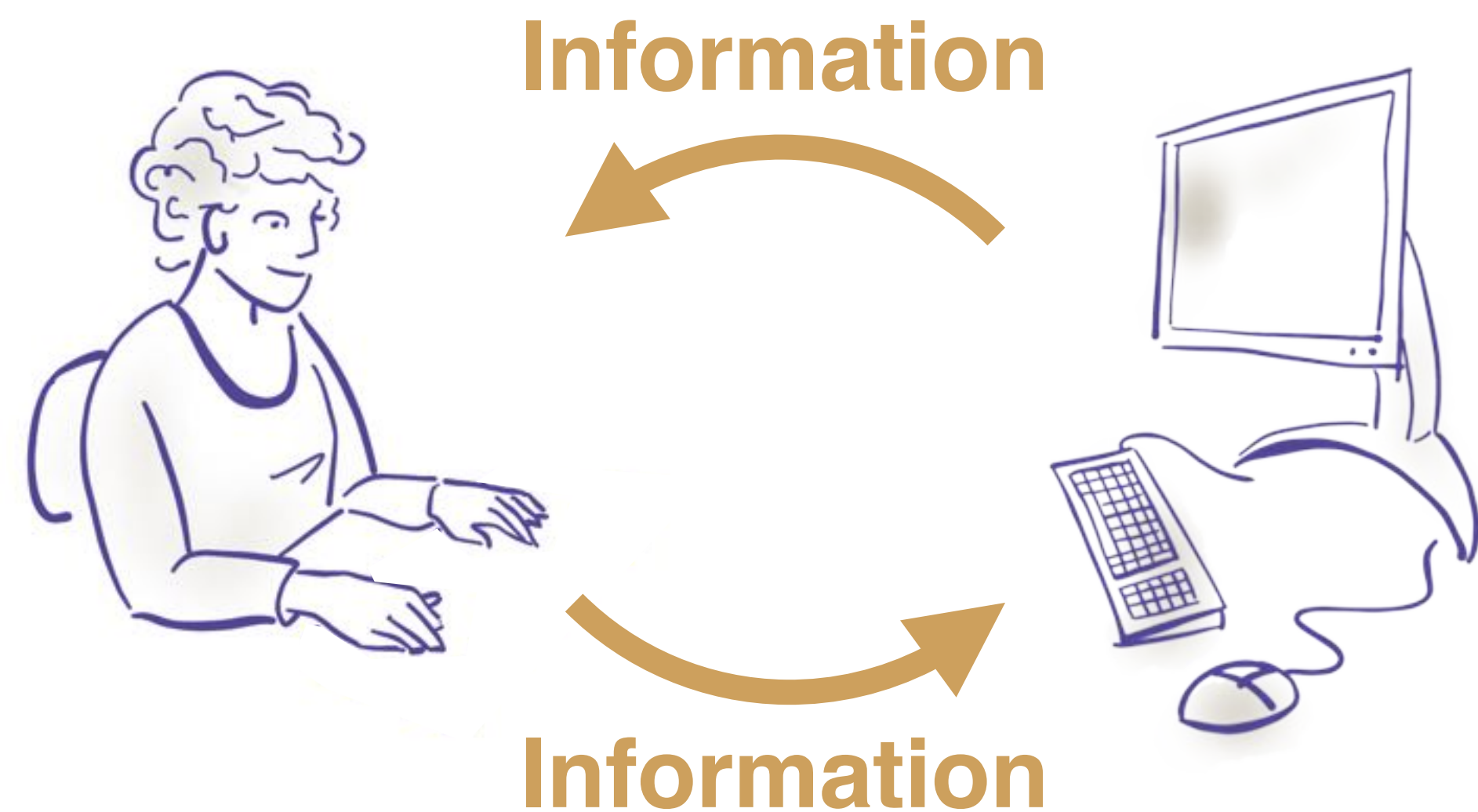
Interaction as a phenomenon



What is sent by the user
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Interaction as a phenomenon



What is sent by the user
to the computer?

What is sent by the computer
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Interaction as
information communication

James Gibson

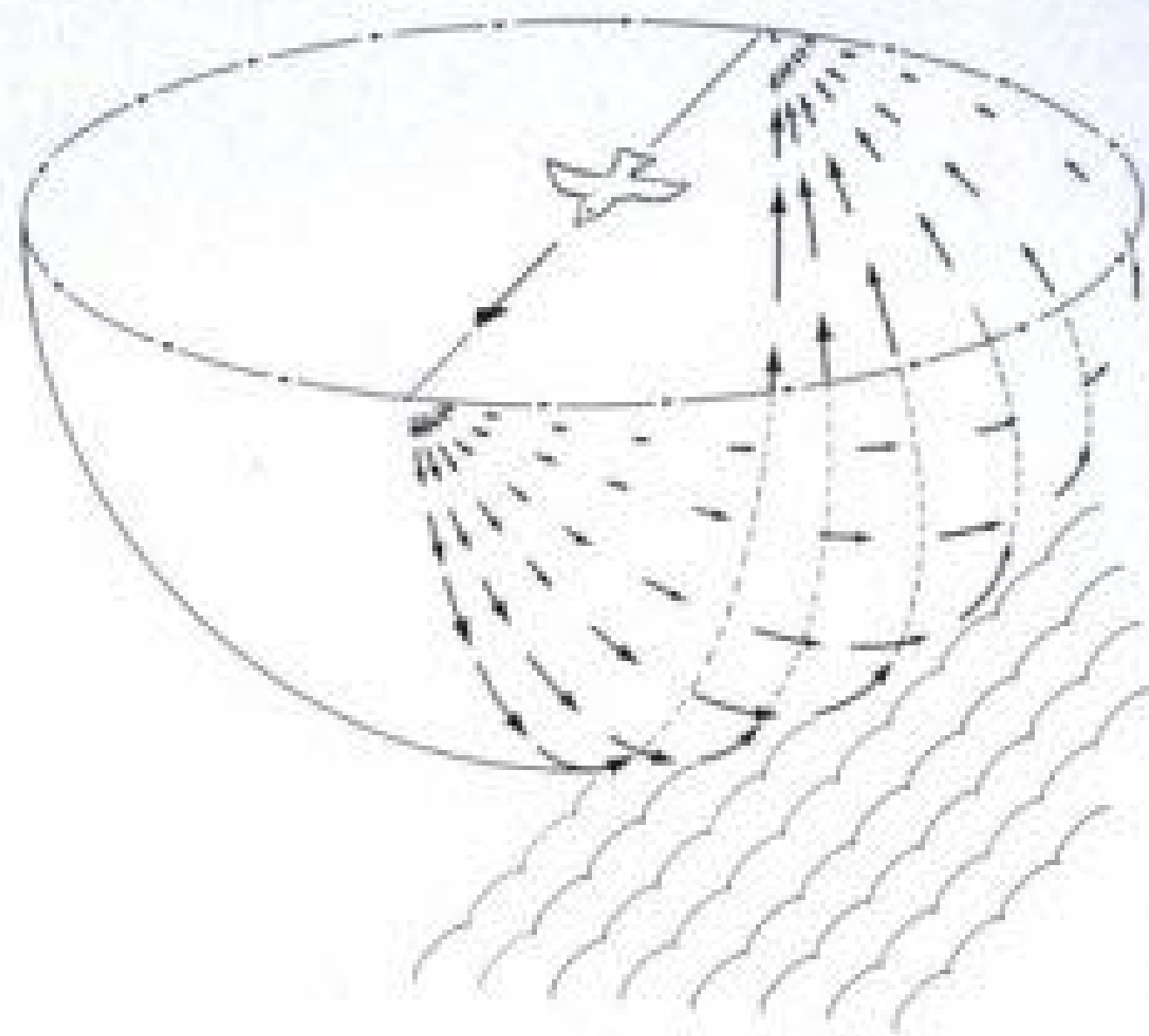
Ecological perception (1979)

Known in HCI for
the notion of “affordance”



THE ECOLOGICAL APPROACH TO VISUAL PERCEPTION

James J. Gibson



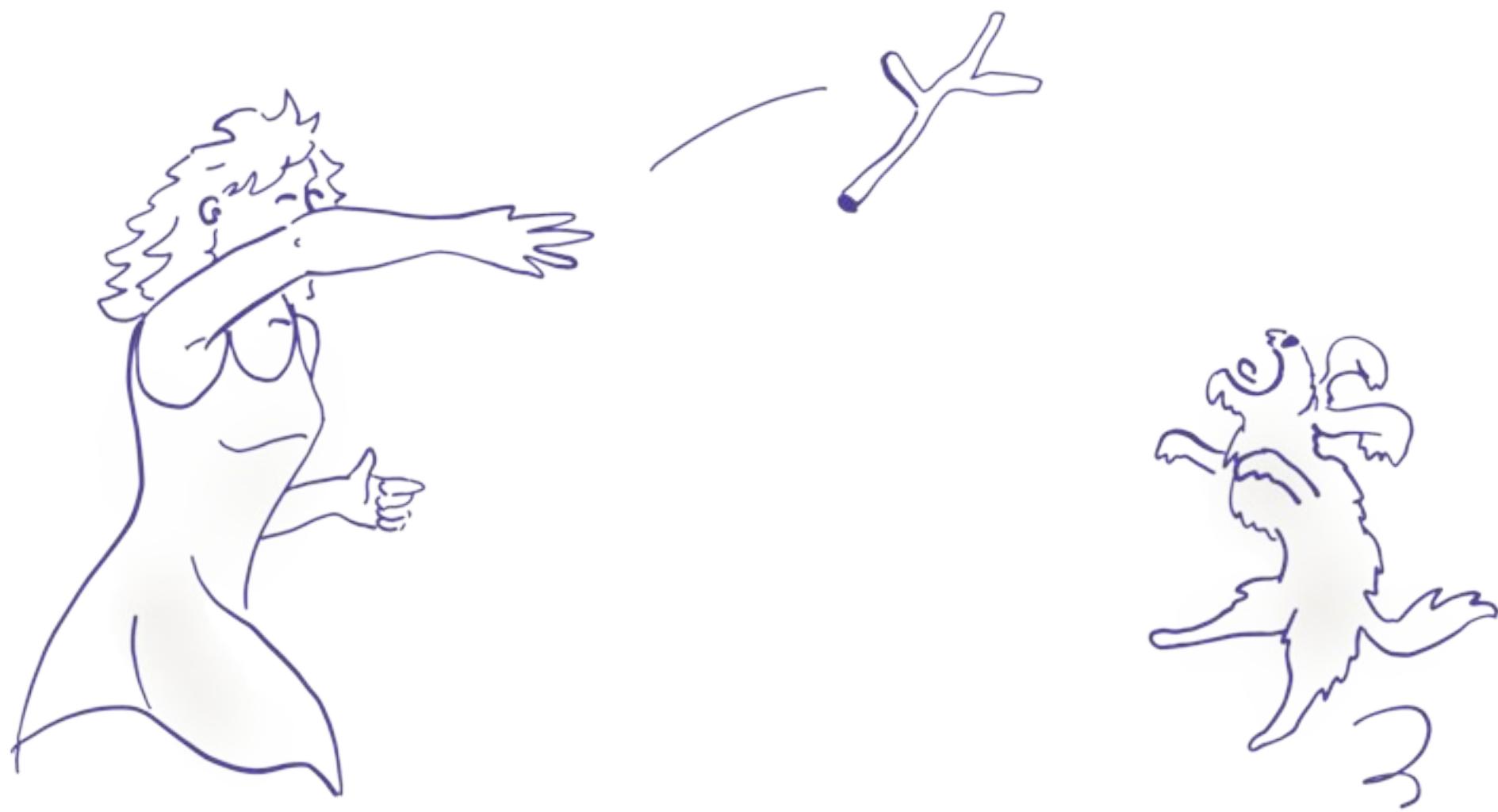
LEA

**Co-evolution between organism
and its environment**

“Elegant” perceptual processes

**Information is in the optical array
and the optical flow**

“Information pickup”

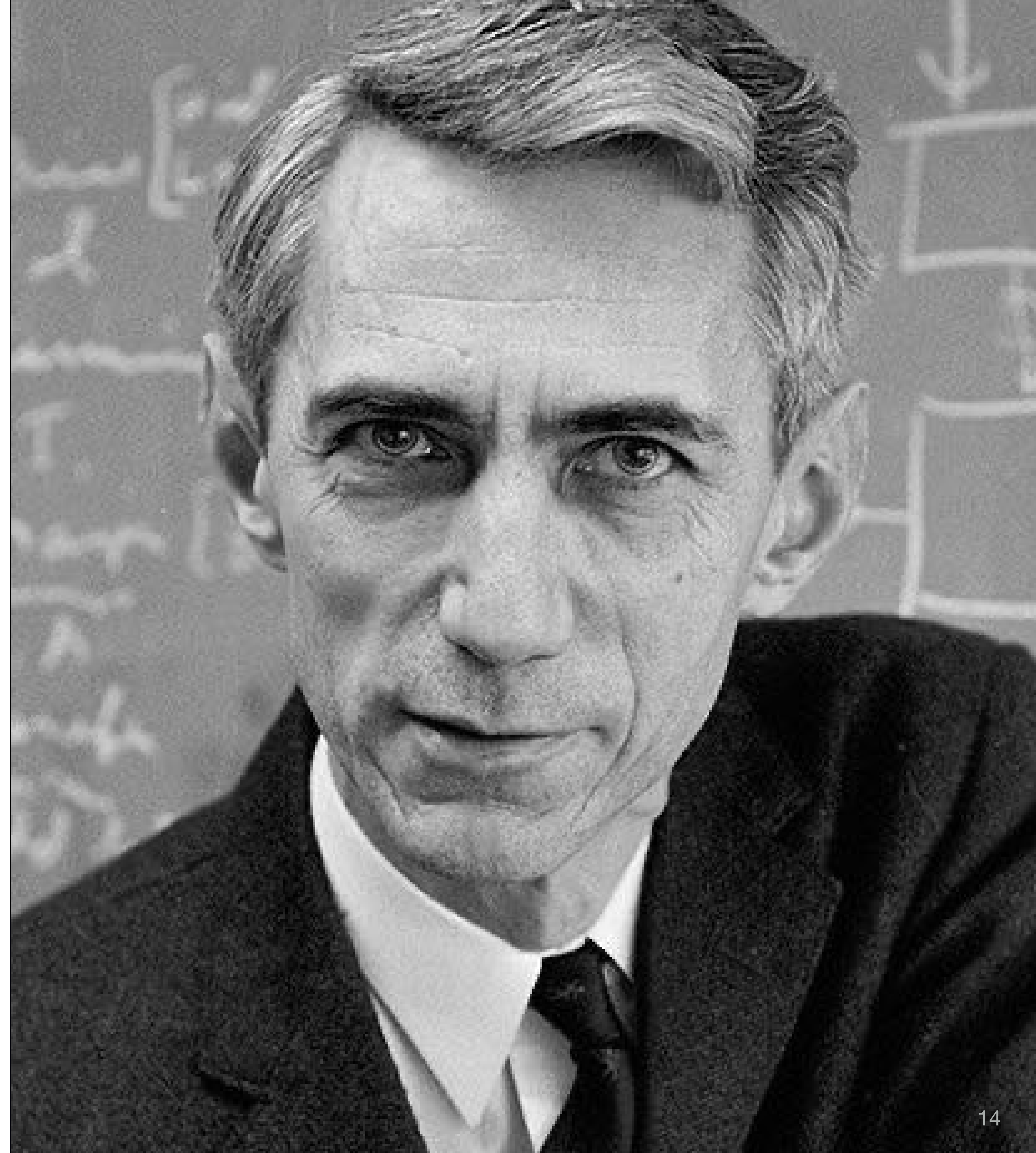


**The organism is equipped to
extract invariants**

**Action-perception coupling
act to perceive
perceive to act**

Claude Shannon

Theory of
information (1948)



Concept of information

Information
reduces
uncertainty

Information carried by an event x
of probability $p(x)$:

$$h(x) = \log_2(1/p(x)) = -\log_2(p(x))$$

Draw a coin: $h(\text{heads}) = 1$ bit

Draw a dice: $h(3) = 2.58$ bits

Concept of entropy

A measure of uncertainty

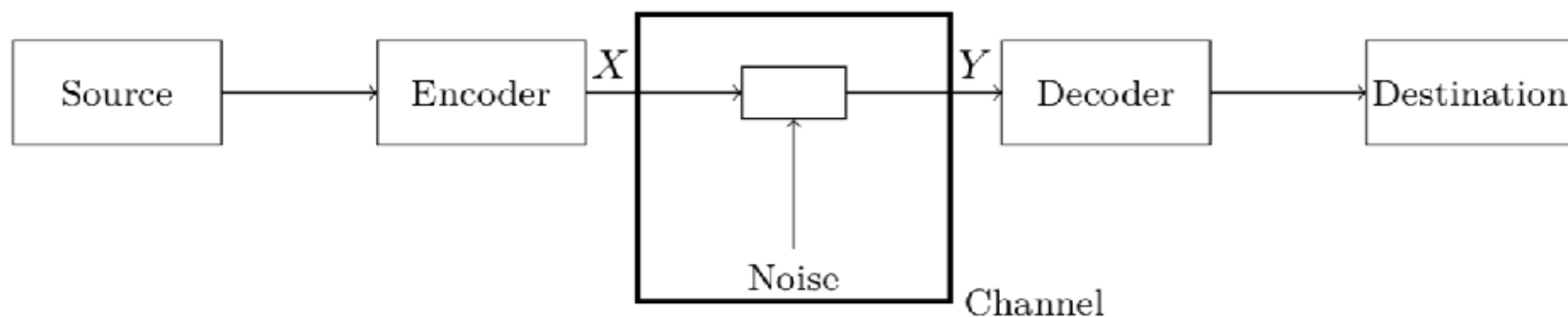
Entropy of a random variable:

$$H(X) = - \sum_x p(x) \log_2 p(x)$$

Entropy is maximal when the distribution $p(X)$ is uniform

English text: entropy between 0.6 and 1.3 bits per character

Information transmission



Entropy of a random variable:

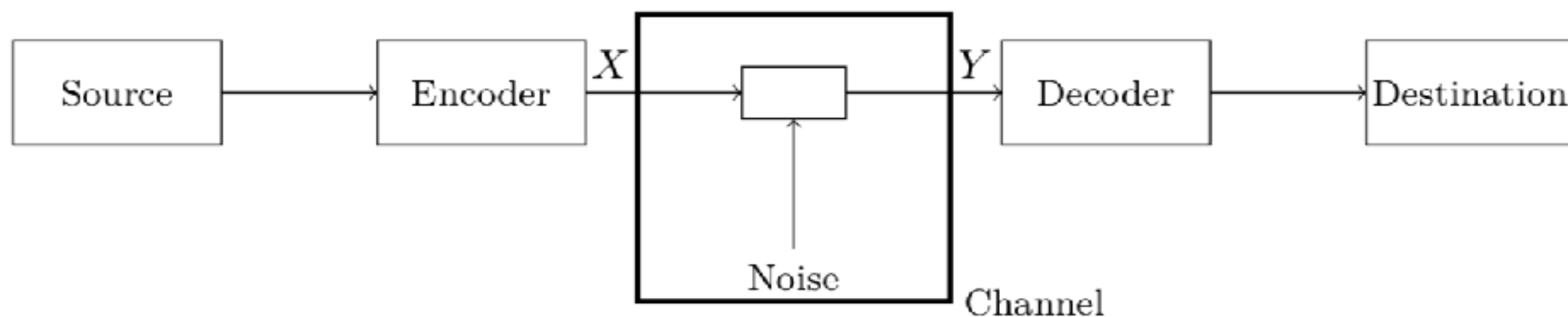
$$H(X) = - \sum_x p(x) \log_2 p(x)$$

Transmitted information:

$$I(X; Y) = H(Y) - H(Y|X)$$

some information is lost

Shannon's theorem 17



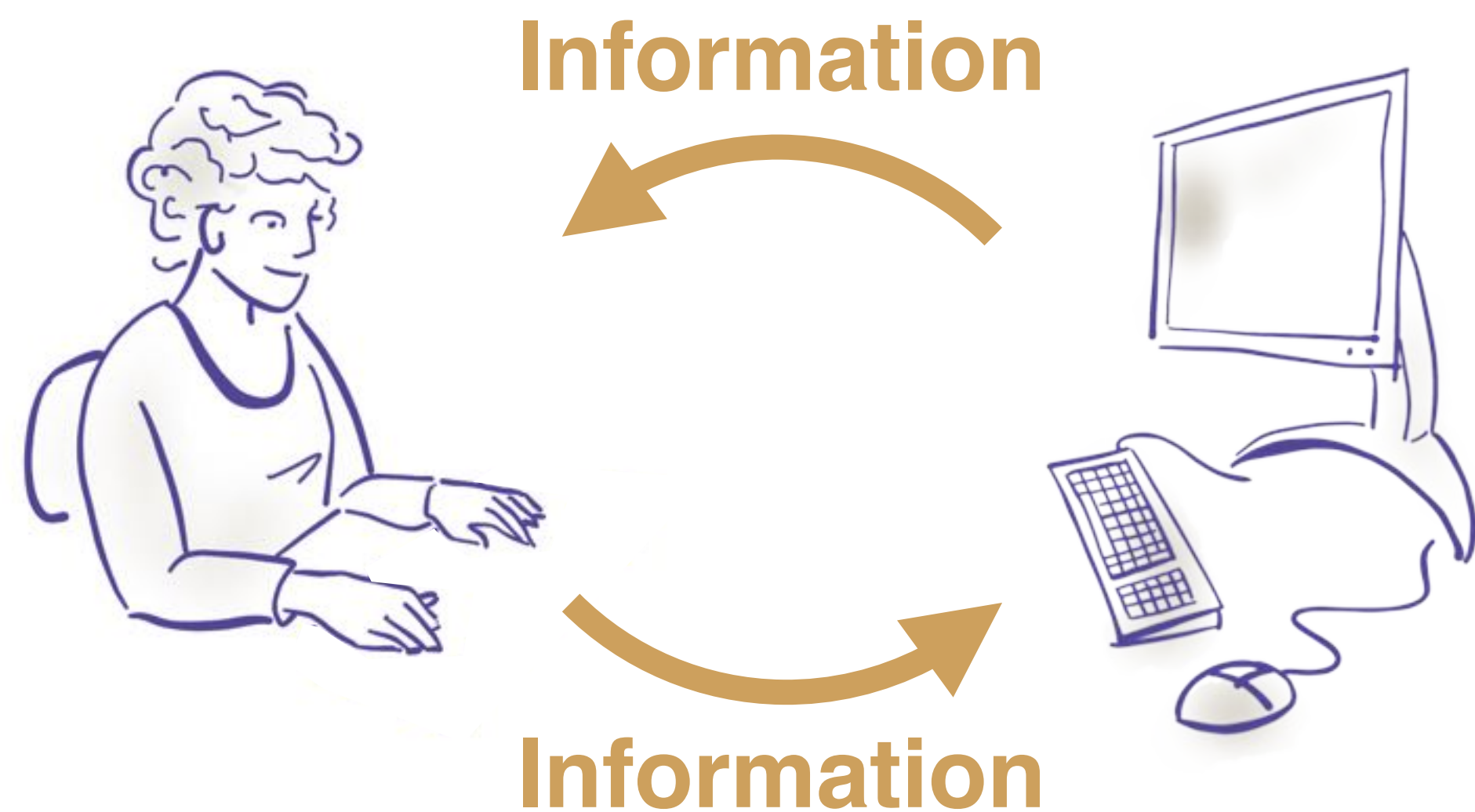
Capacity of a channel
subject to Gaussian noise:

$$C = B_W \log_2 \left(1 + \frac{P}{N} \right)$$

C is measured in bits/second

Maximum transmitted information

What information?



User -> computer
message (commands)
-> Shannon

Computer -> User
view
-> Gibson

Pointing



Pointing



The most frequent task in GUIs

Many targets, some very small

Trade-off between speed and precision

Cost of error can be high

Pointing



If the computer knew where I want to point, it could do it for me

Pointing performance is limited by human capabilities

Paul Fitts

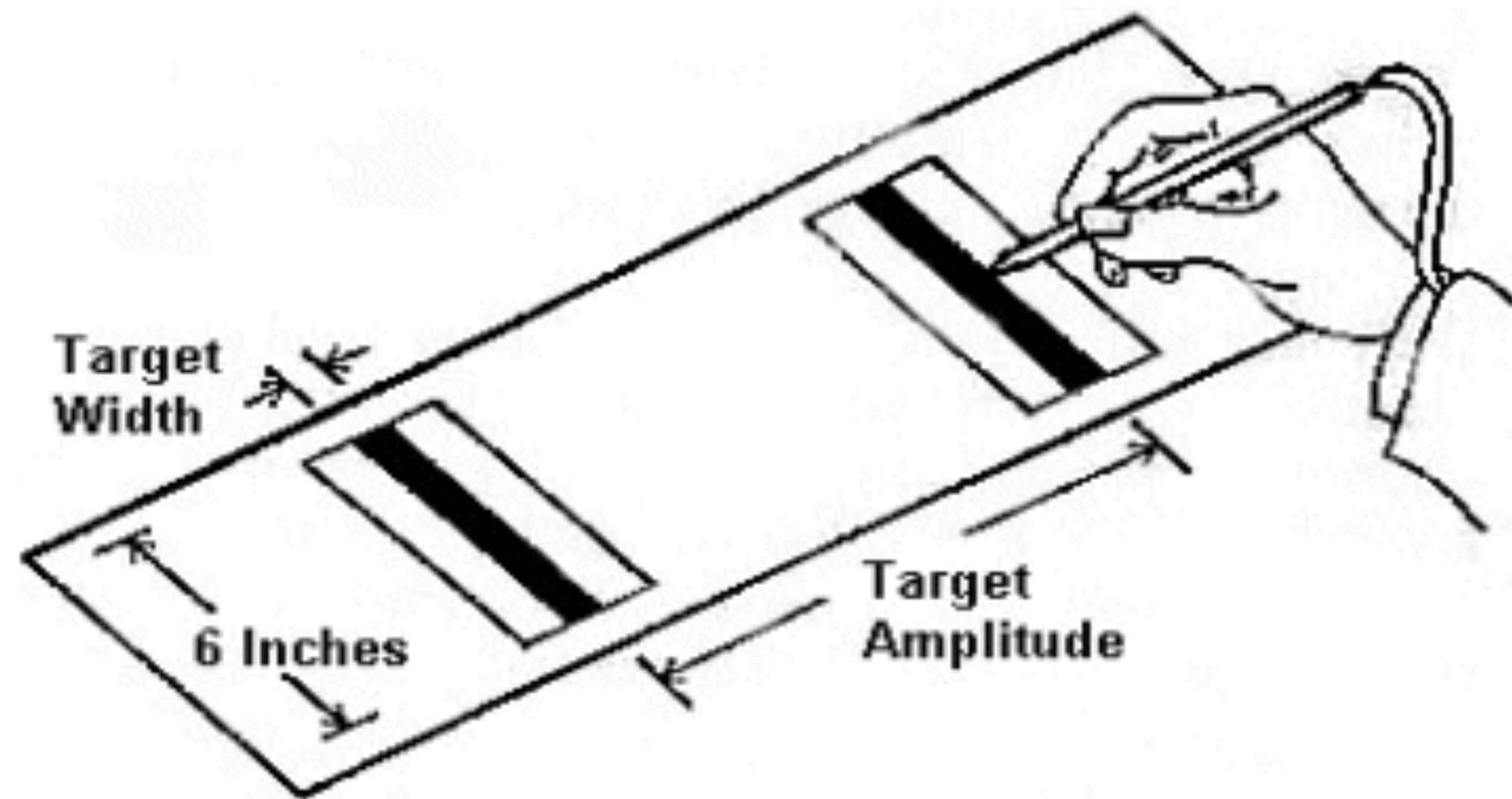
Psychologist

Also a pioneer in
aviation safety

HAGA-MAGA list



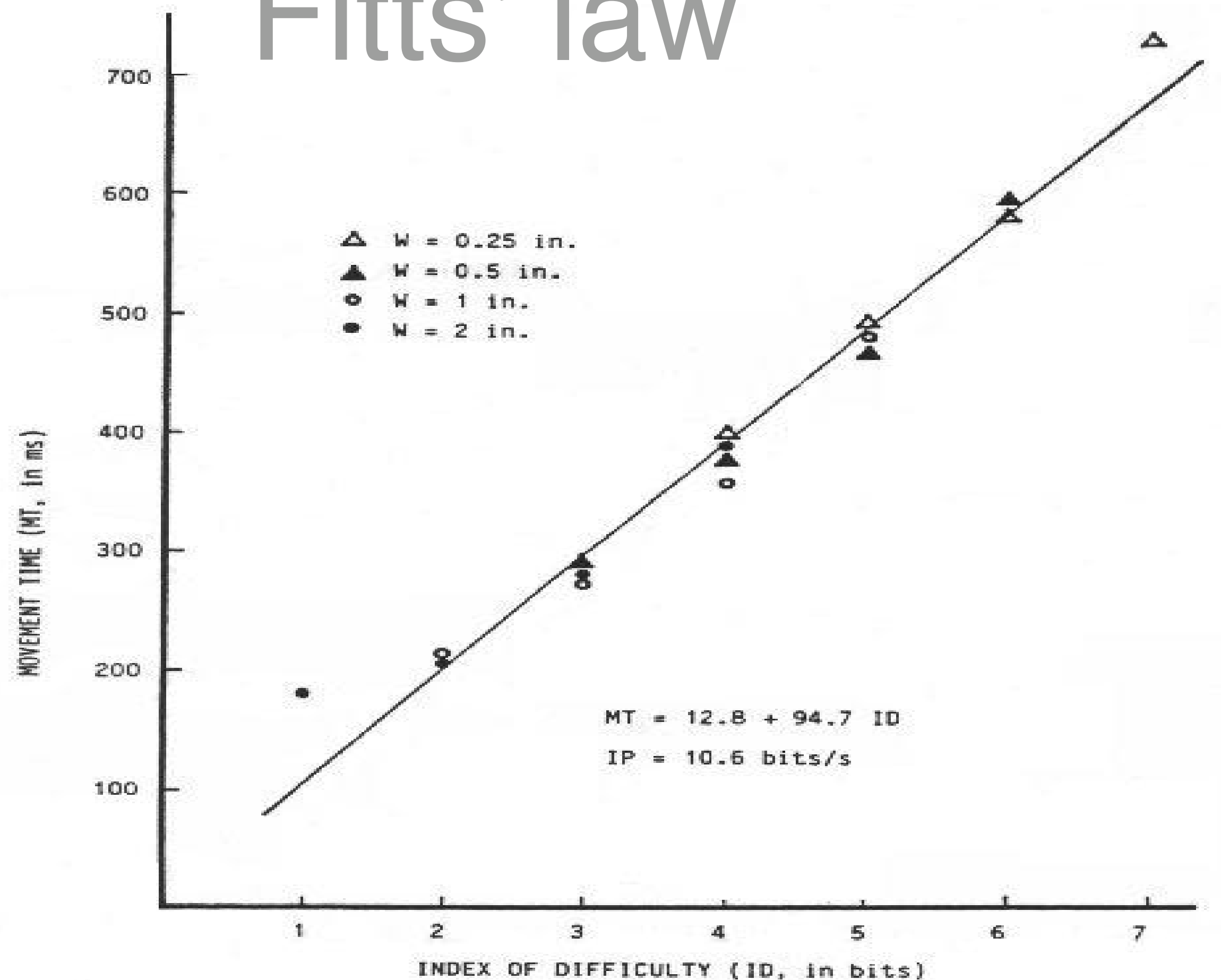
Fitts' law (1954)



Speed-precision trade-off
in aimed movements

D = distance to target
 W = target width

Fitts' law



Speed-precision trade-off
in aimed movements

D = distance to target

W = target width

MT = k x ID movement time

ID = $\log(1 + D/W)$ index of difficulty

Fitts' law

A tool to compare
pointing devices or
pointing techniques

Speed-precision trade-off
in aimed movements

D = distance to target

W = target width

$MT = k \times ID$ movement time

$ID = \log(1 + D/W)$ index of difficulty

Shannon meets Fitts

Parallel between

$$MT = k \log_2 \left(1 + \frac{D}{W} \right)$$

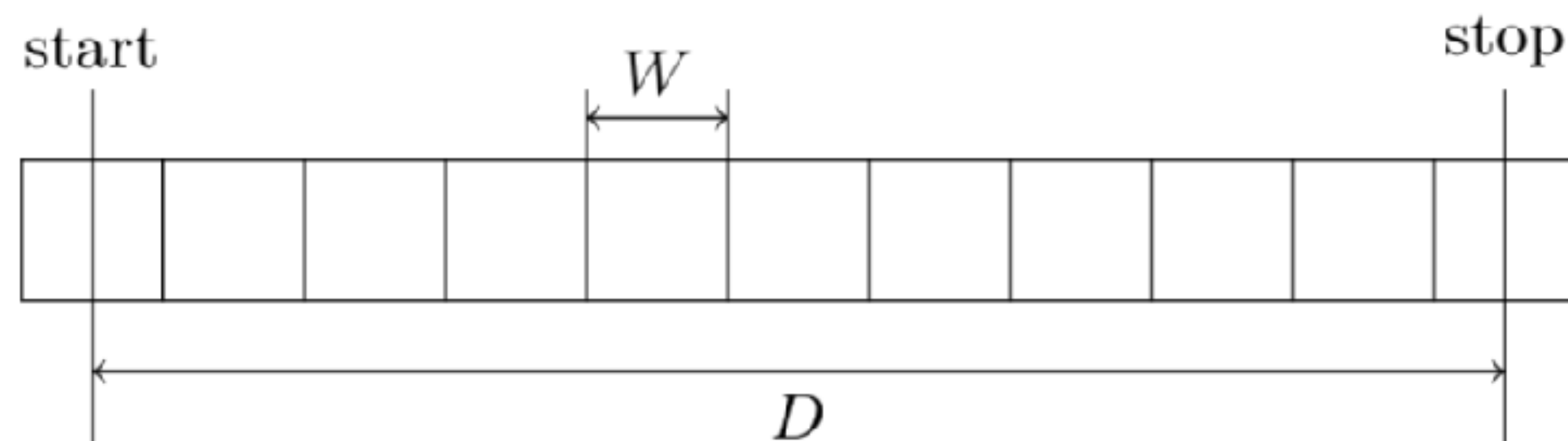
and

$$C = B_w \log_2 \left(1 + \frac{P}{N} \right)$$

Distance = Signal

Width (tolerance) = Noise

Shannon meets Fitts



Aiming is choosing

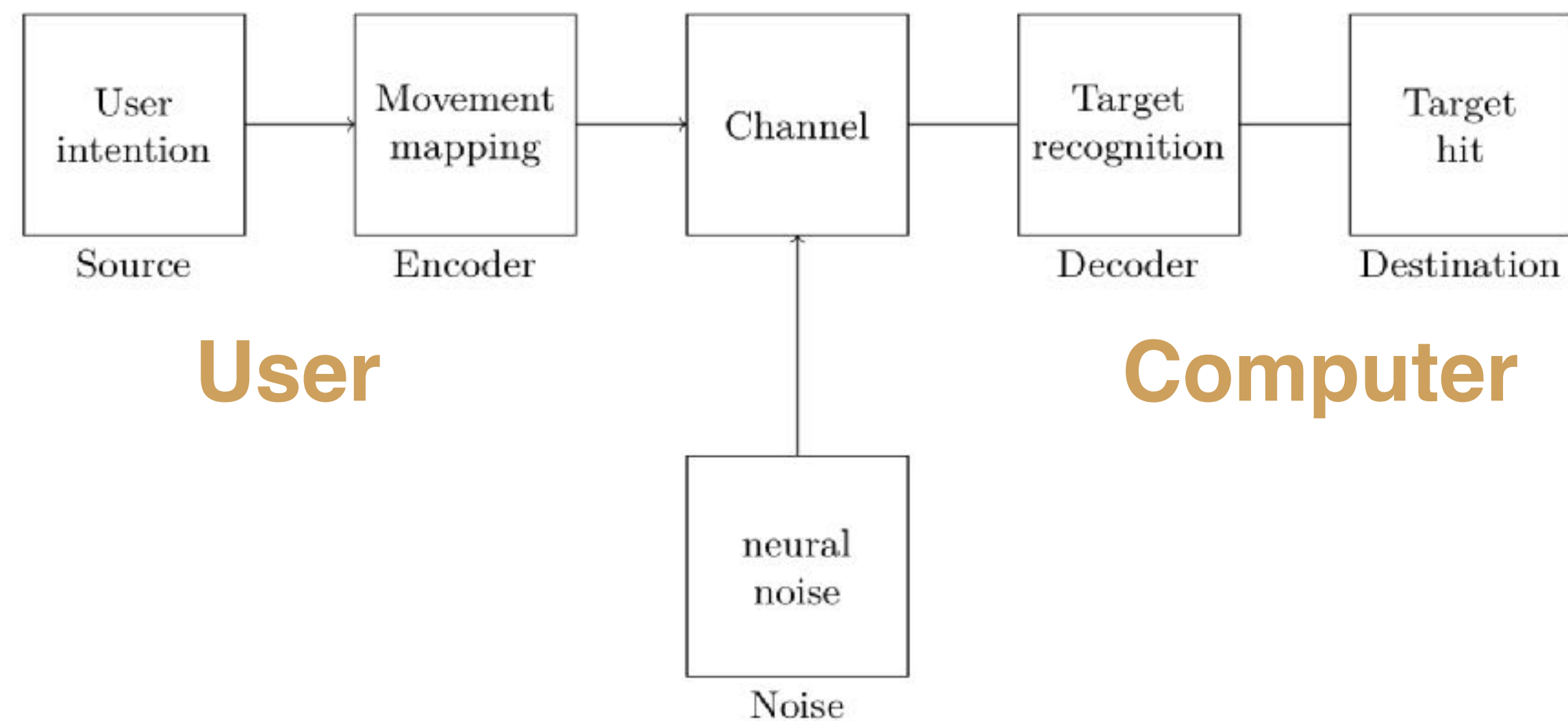
$$X = -\frac{D}{2}, -\frac{D}{2} + W, \dots, \frac{D}{2} - W, \frac{D}{2}$$

$$H = \log_2 \left(1 + \frac{D}{W} \right) = ID$$

Index of difficulty = source entropy

No transmission!

Shannon meets Fitts



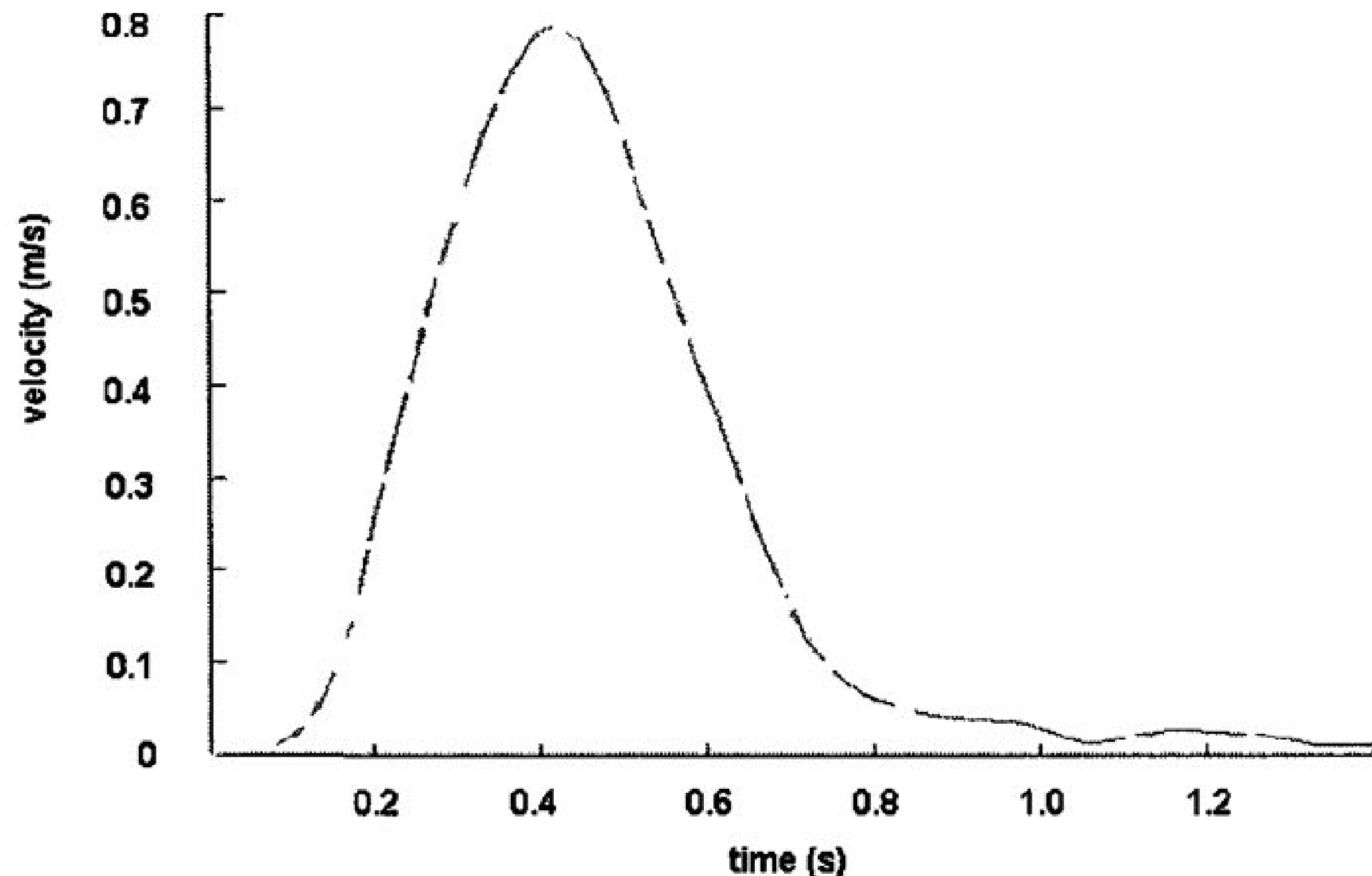
Gori, Rioul & Guiard, 2018

Modeling the motor system as the
(noisy) channel

If e is the error rate

$$C = (1 - e) \log_2 \left(1 + \frac{D}{W} \right)$$

Limits of Fitts' law



First, ballistic movement,
followed by corrective movements

Validity of the law

Distance < amplitude of the arm

Target size > motor tremor

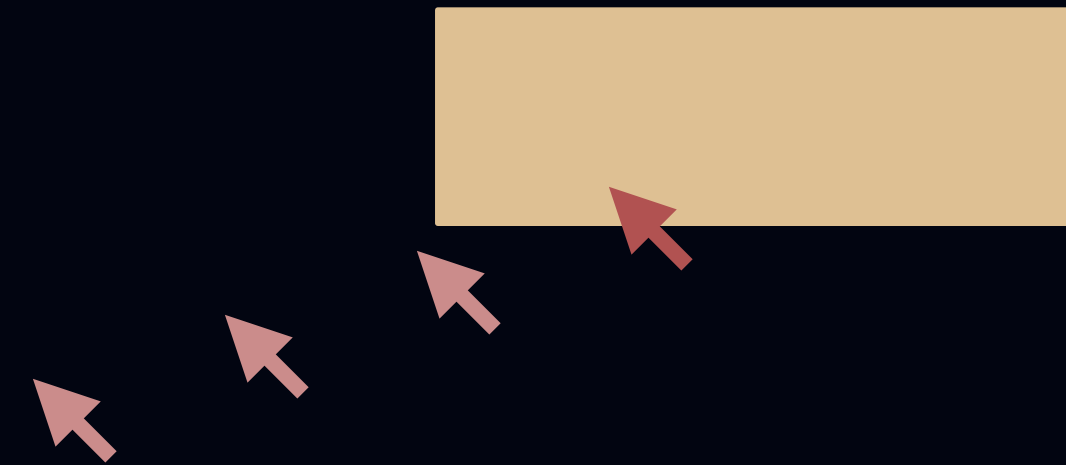
Distance < ~1m

Target size > ~0.5mm

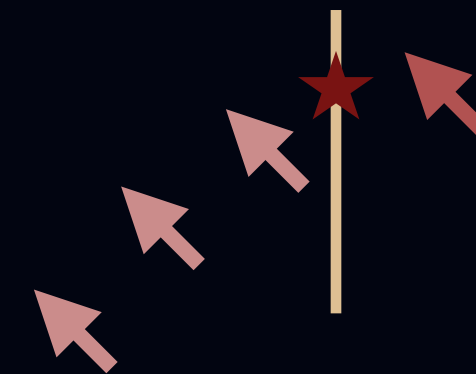
ID < ~11 bits

Other laws of movement

Fitts' law in 2D



Goal passing / crossing (Accot & Zhai)



The Steering law (Accot)



“Beating” Fitts’ Law

How can the system
help the user
reach the target faster?

Pointing as
human-computer partnership

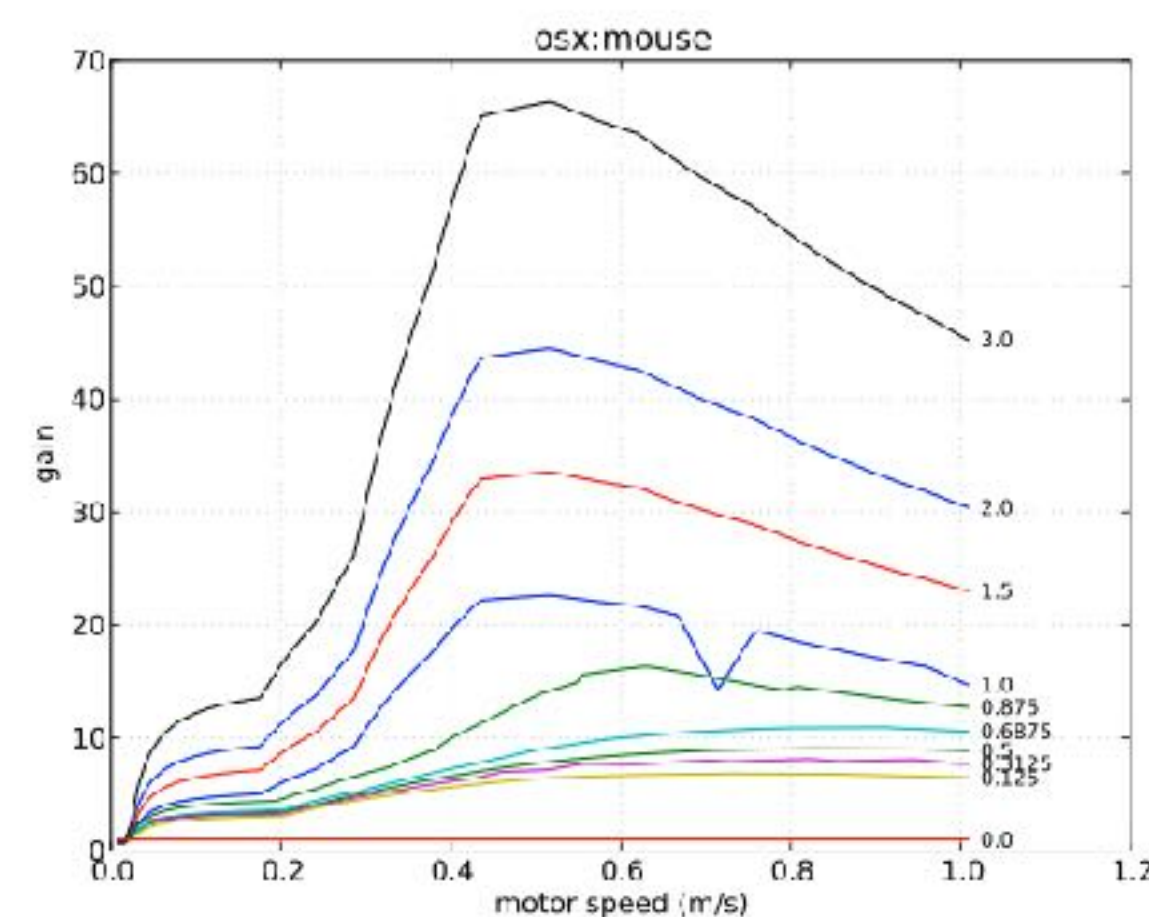
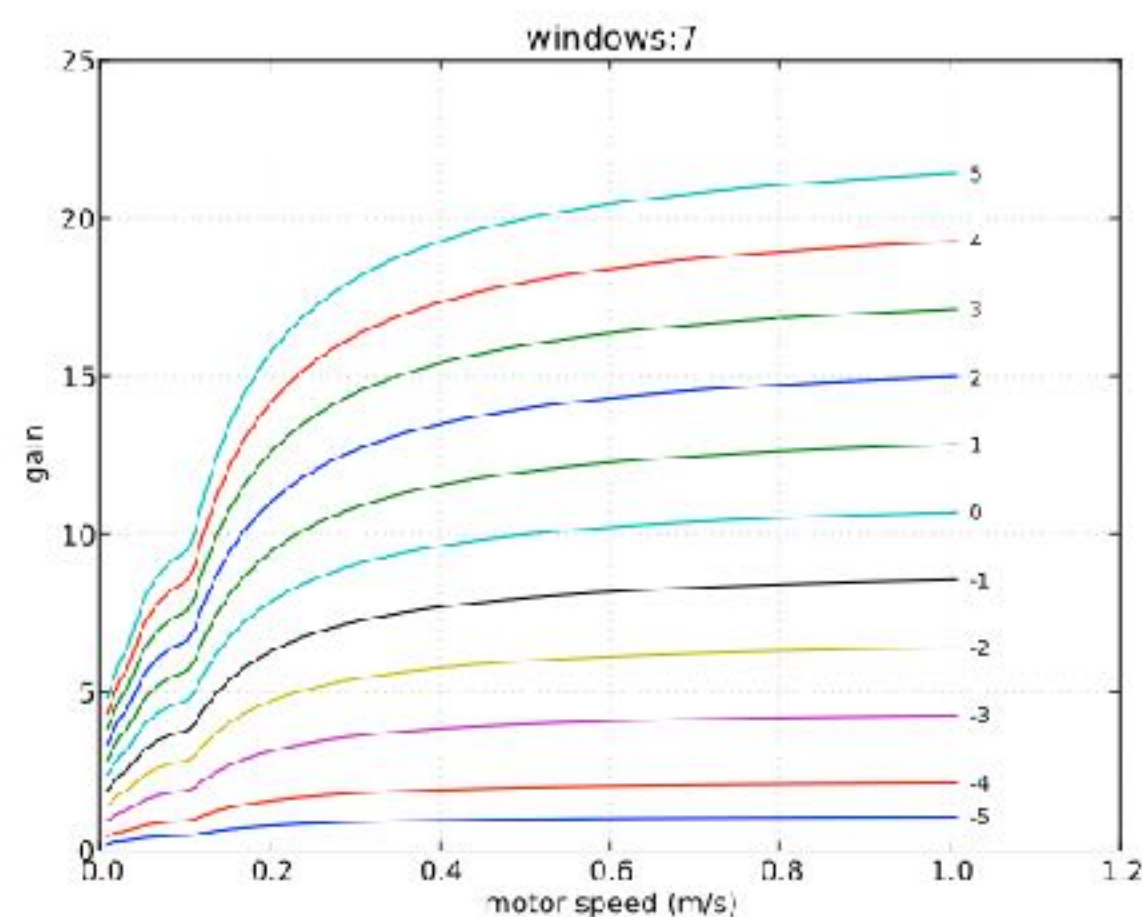
“Beating” Fitts’ Law

How can the system
help the user
reach the target faster?

1. Extract user intention

Pointer acceleration Transfer function

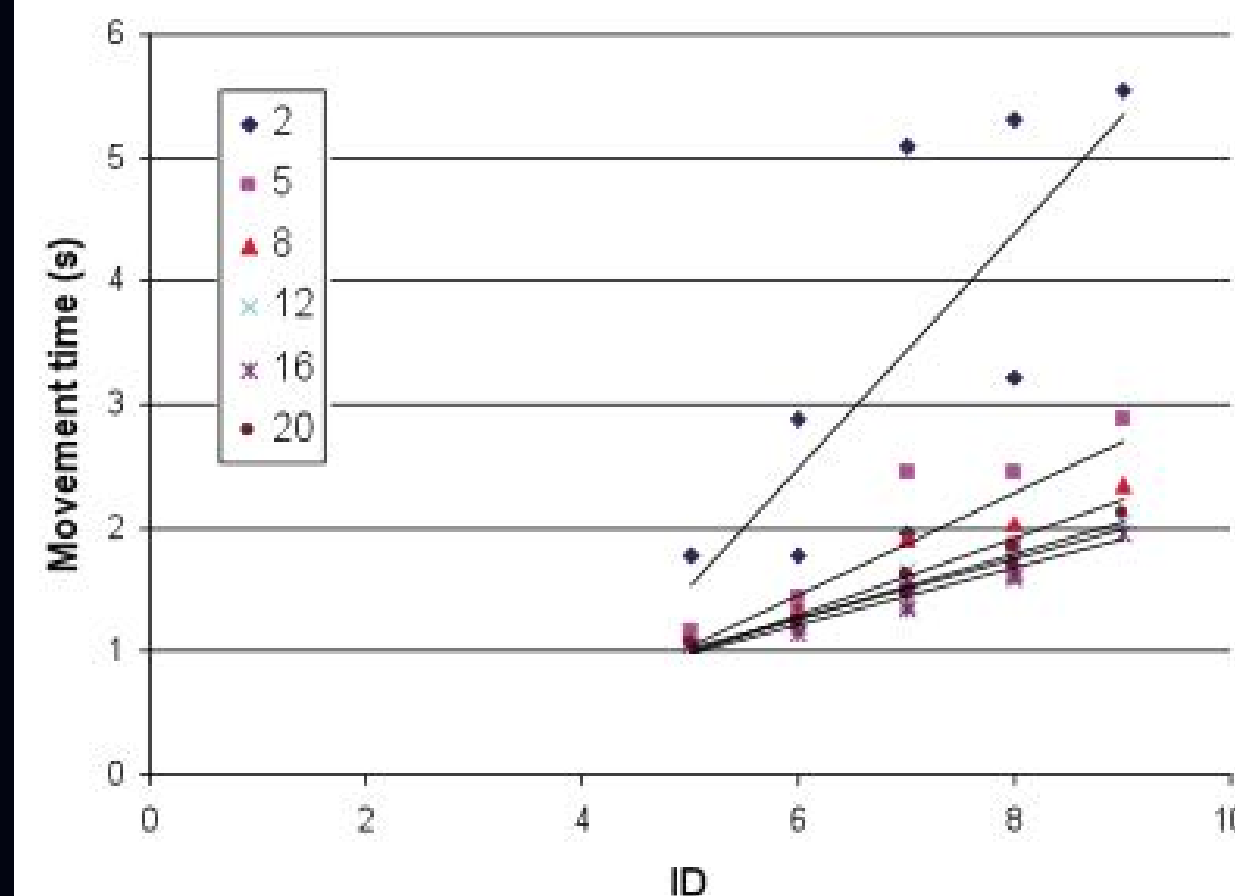
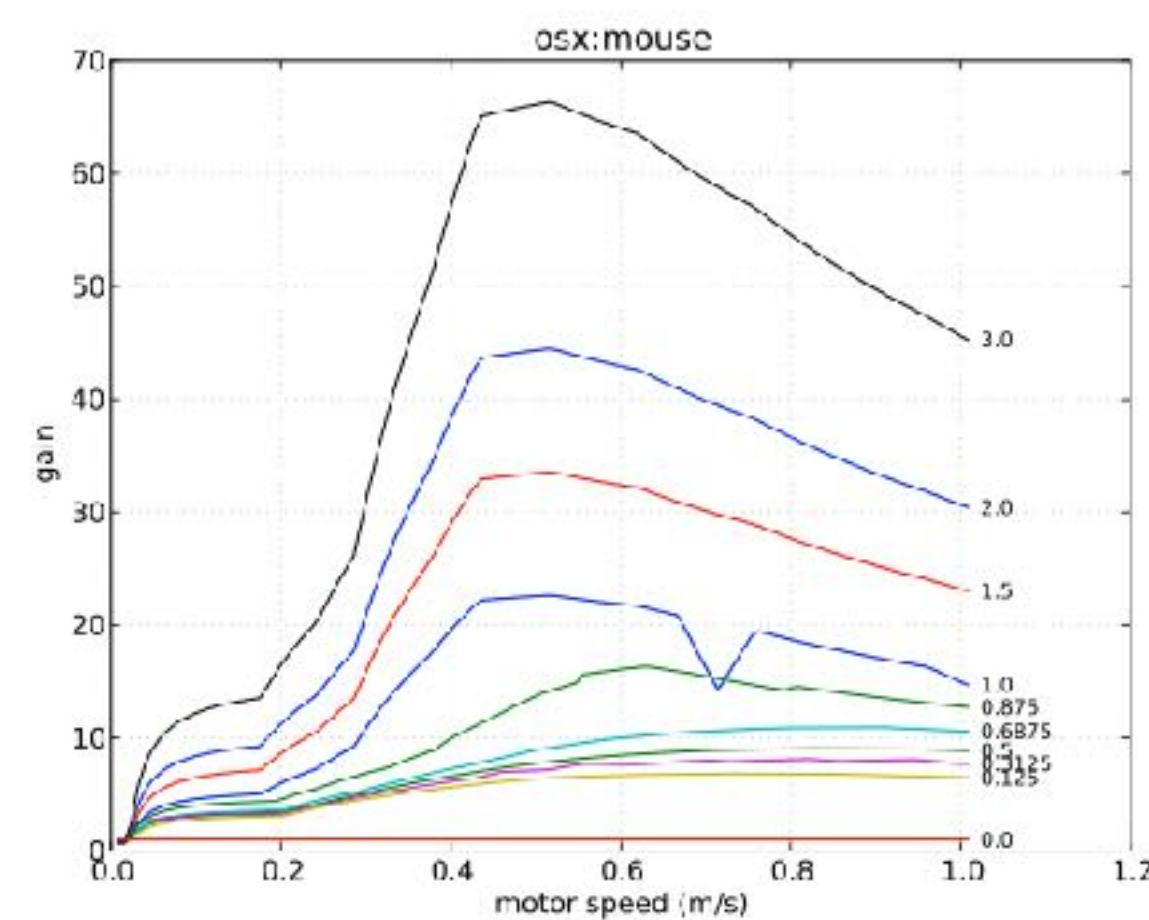
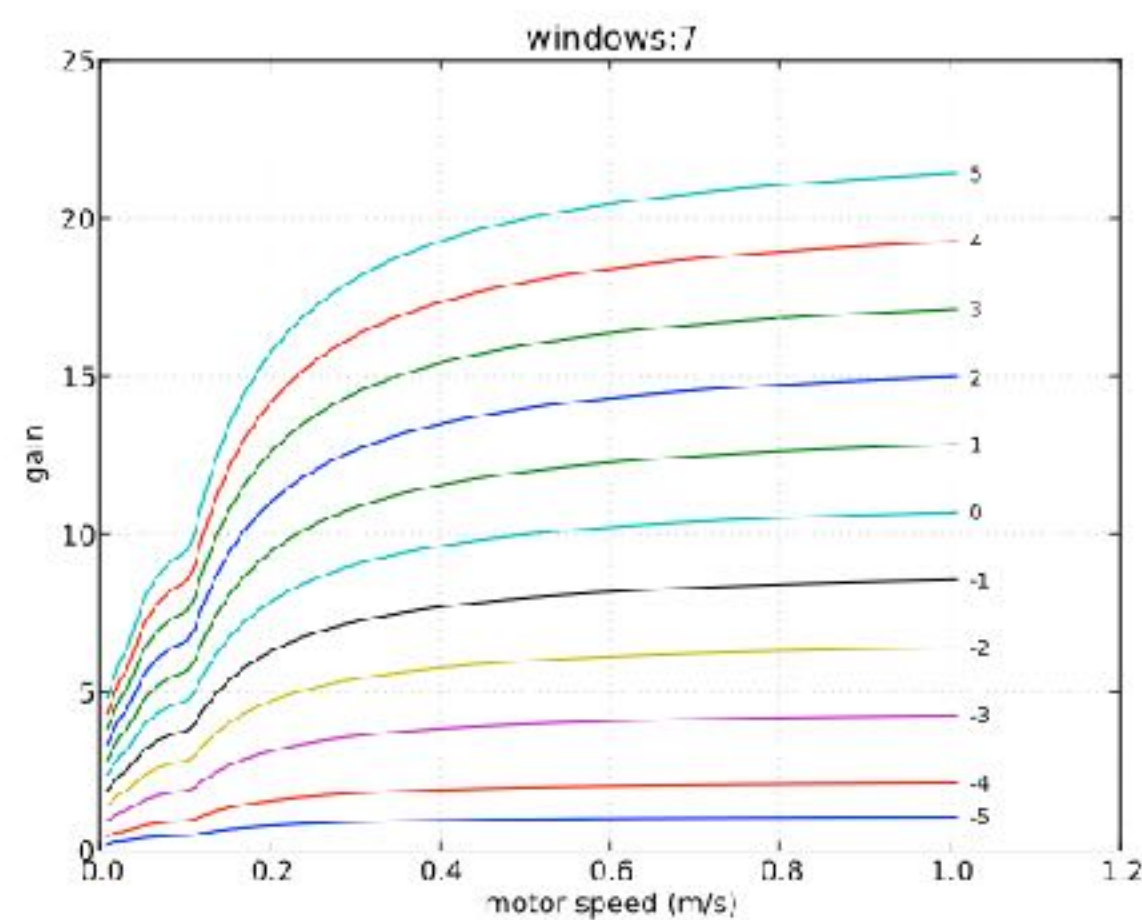
Move the cursor proportionally
faster when the mouse moves
faster:
moving fast means wanting to go
further away



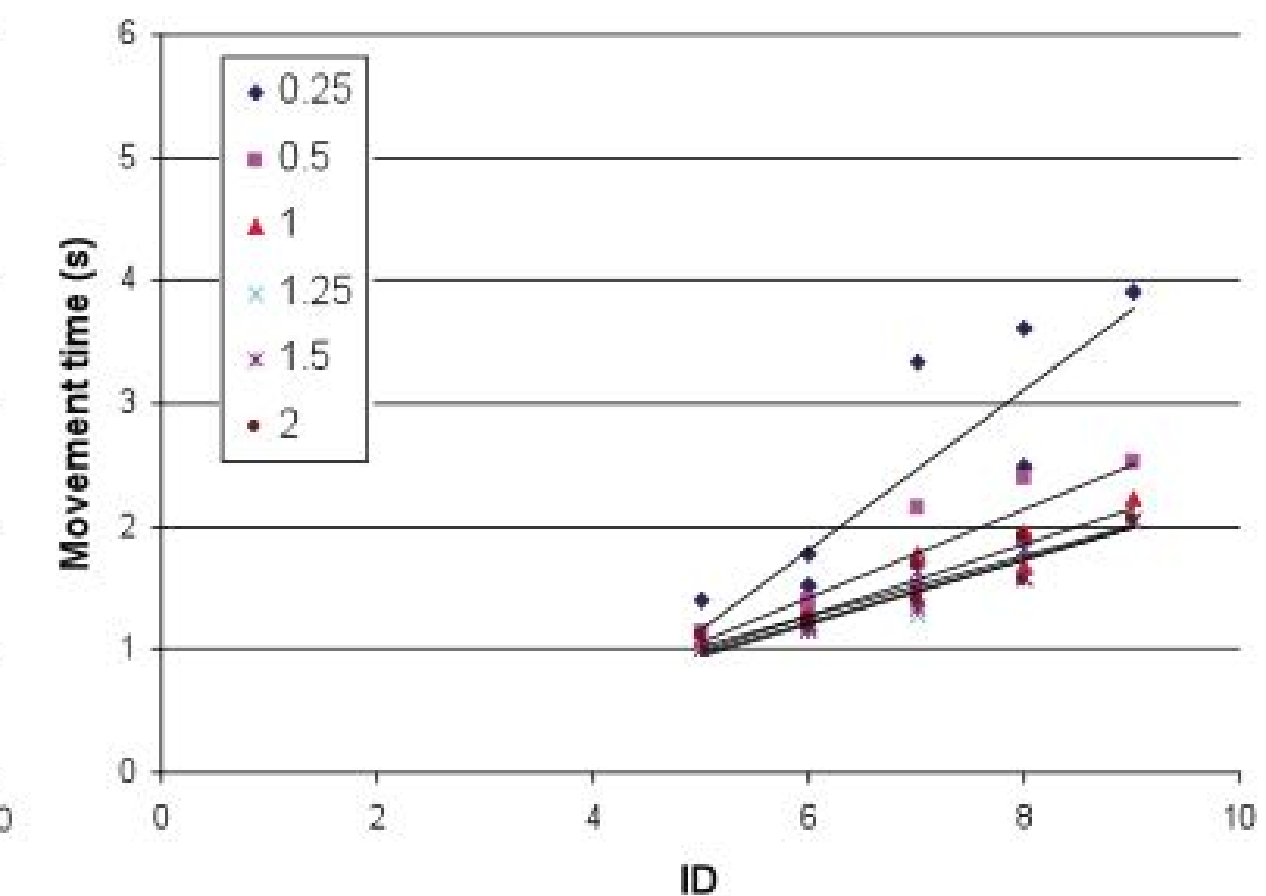
Casiez et al., 2008

Pointer acceleration Transfer function

Real but moderate effect
on performance



(a) Constant Gain



(b) Pointer Acceleration

Gliding cursor



Beaudouin-Lafon et al., 2014

Cursor with inertia

**Similar to scrolling a list
on a smartphone**

**Does not improve pointing time
BUT
user controls the cursor only
part of the time**

“Beating” Fitts’ Law

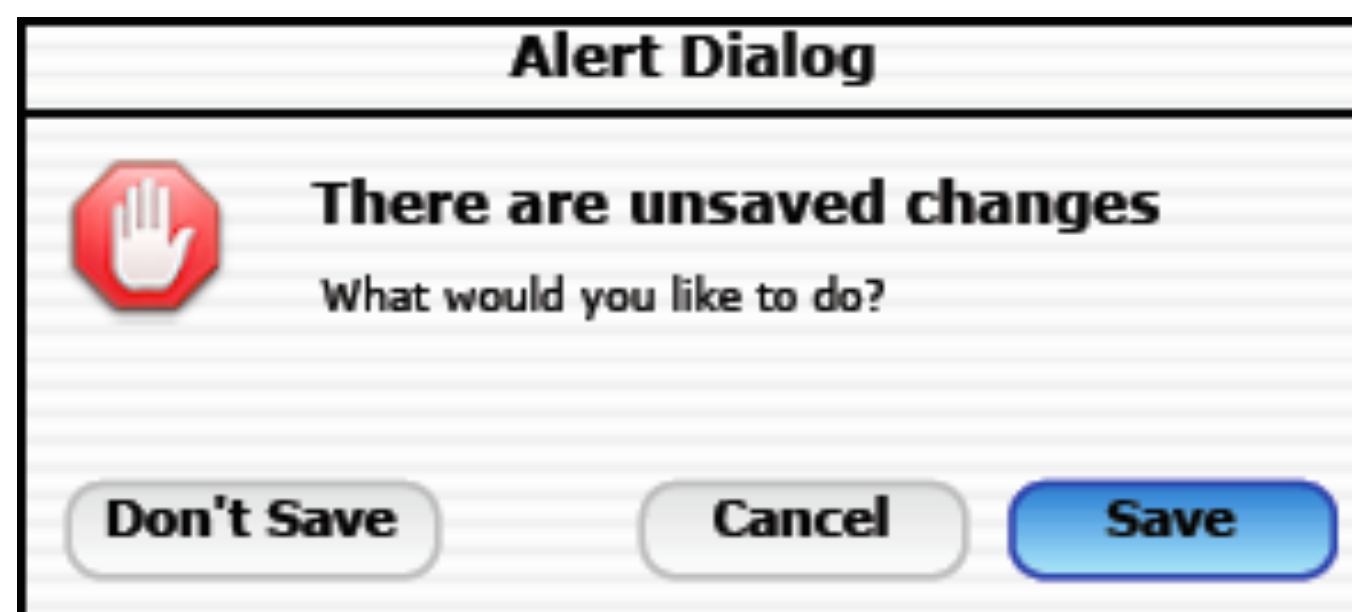
How can the system
help the user
reach the target faster?

1. Extract user intention
2. Use information about targets

Semantic pointing

**Adapt the transfer function to
the “landscape” of targets:
higher gain in the space
between targets**

Semantic pointing



Adapt the transfer function to the “landscape” of targets: higher gain in the space between targets

Visual space



Semantic pointing



Blanch et al., 2004

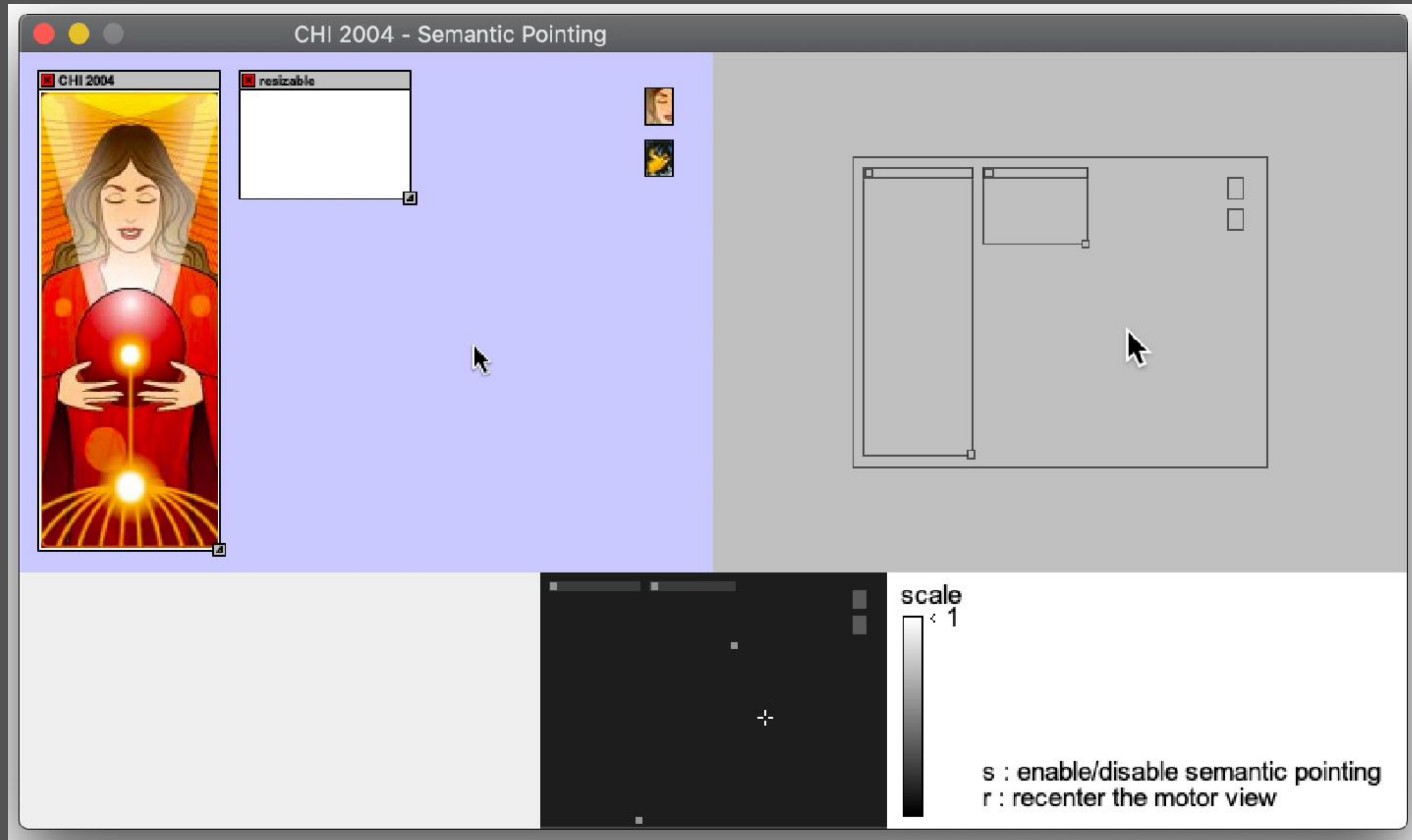
Adapt the transfer function to the “landscape” of targets: higher gain in the space between targets

Visual space



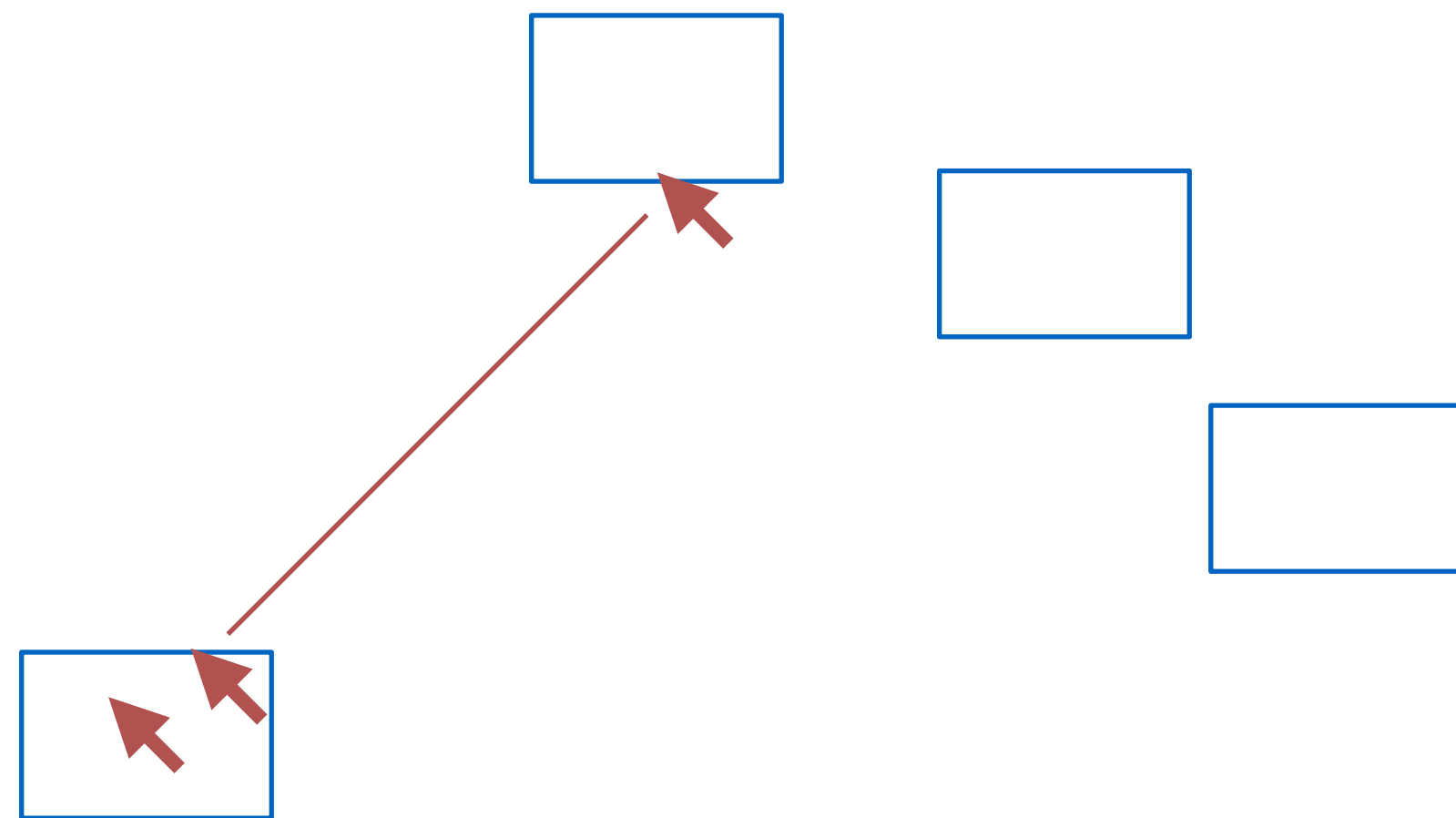
vs. Motor space





Semantic Pointing - Guiard, Blanch & Beaudouin-Lafon, 2004

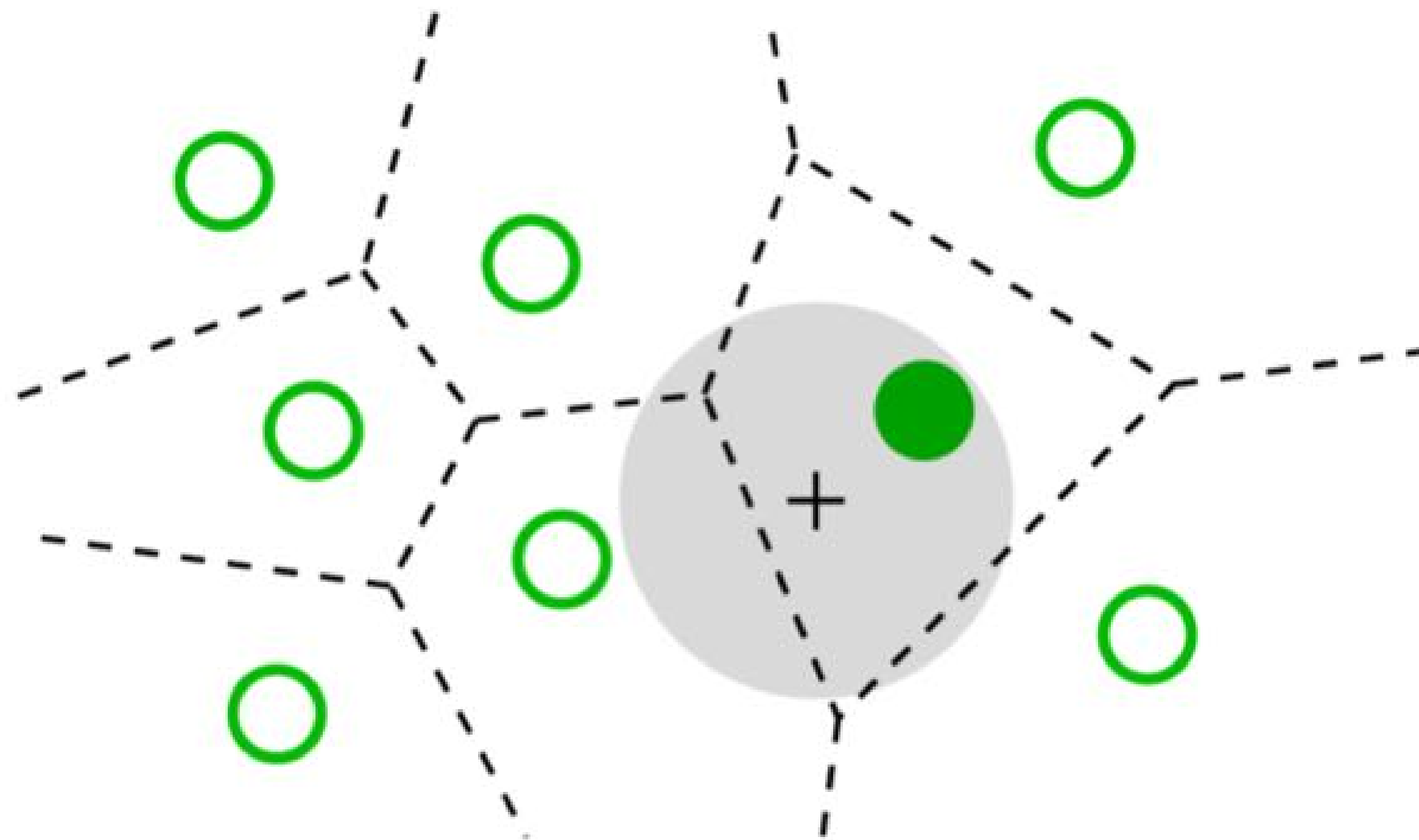
Object pointing



Extreme version of Semantic Pointing:
the cursor ignores empty space and jumps from one target to the next

Problem:
error correction is costly

Bubble pointer



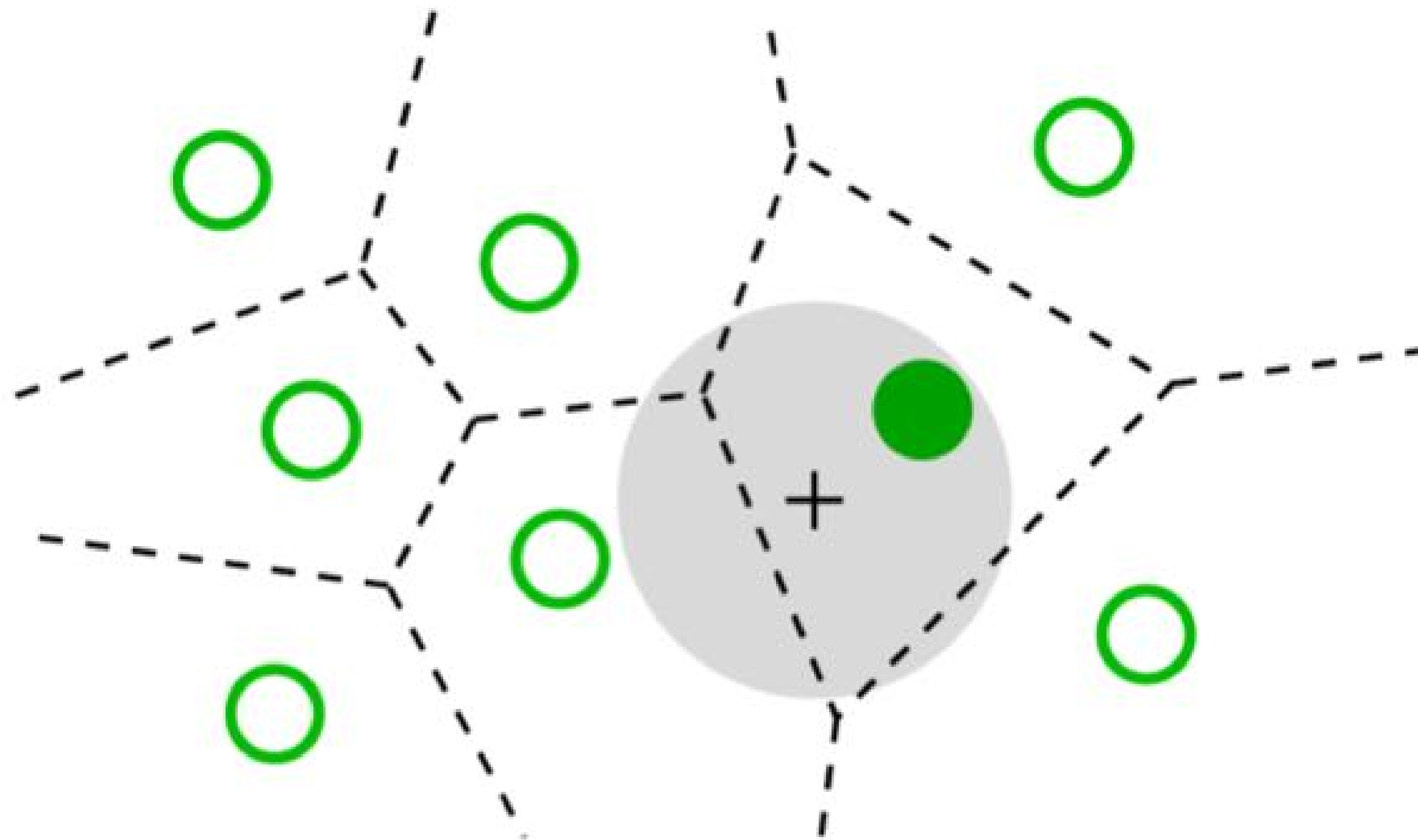
Grossman & Balakrishnan, 2005

**Similar idea to Object Pointing:
eliminate empty space**

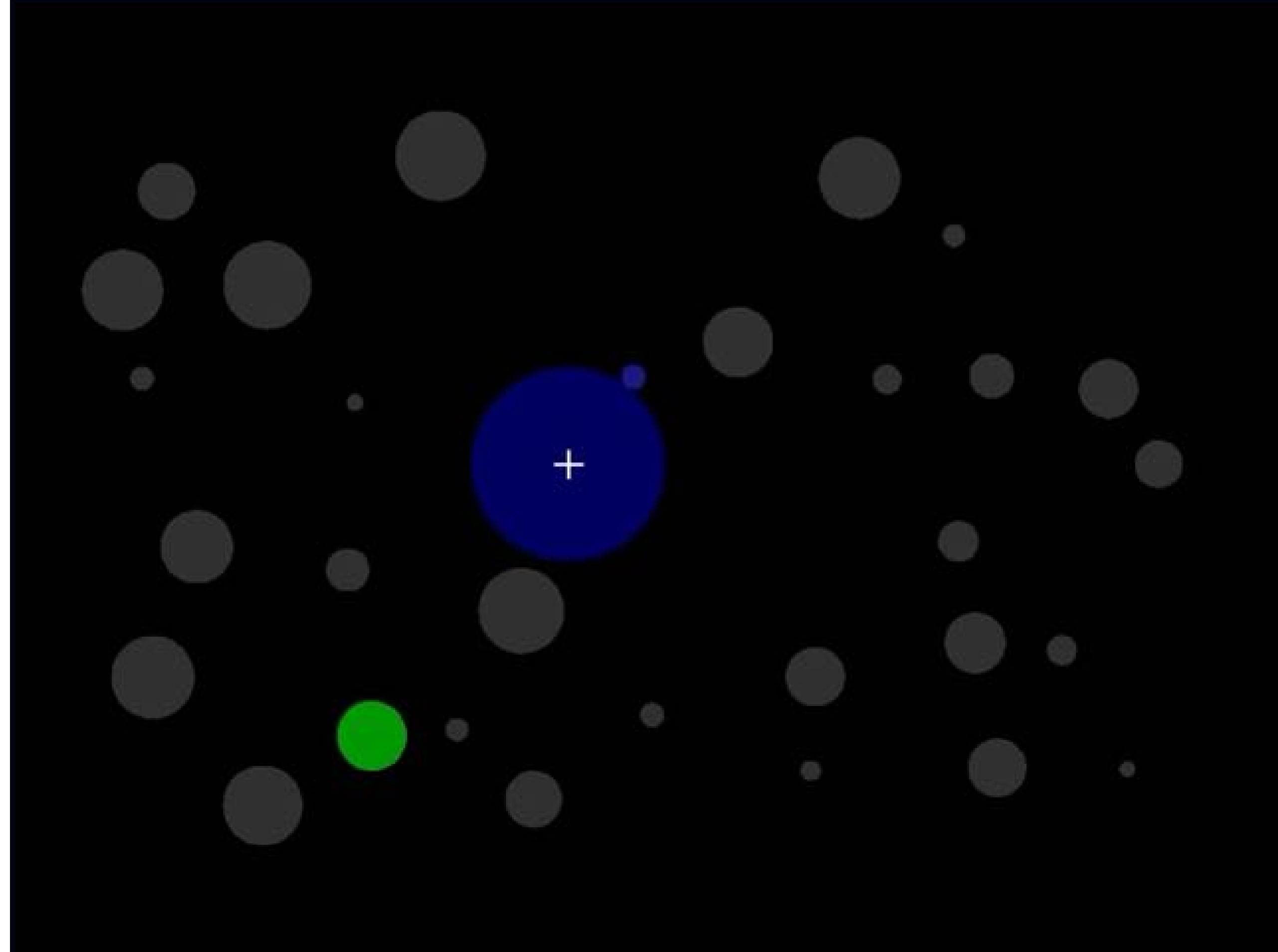
**Any click is a click
on the nearest target**

**Based on the Voronoi diagram
of target positions:
targets are effectively
as big as possible**

Bubble pointer



Grossman & Balakrishnan, 2005



Expanding targets

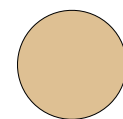


Targets grow
when close to cursor

Pointing time predicted
by expanded target size

McGuffin & Balakrishnan, 2002
Zhai et al., 2003

Expanding targets

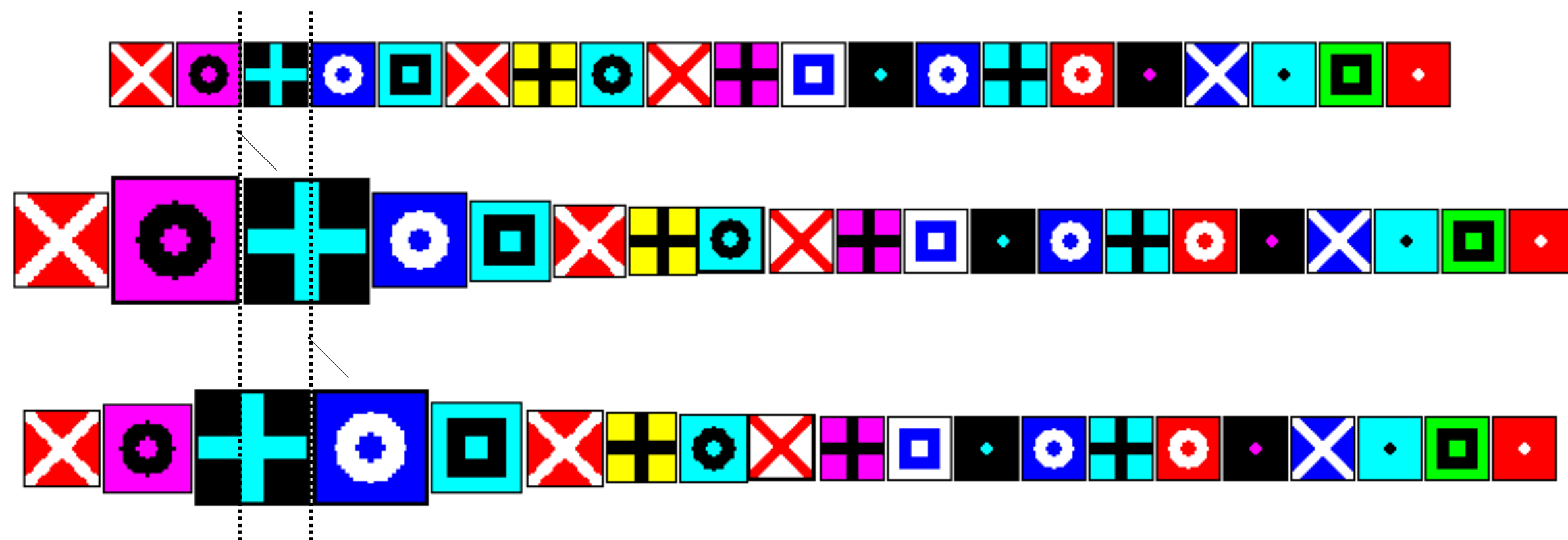


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Expanding targets

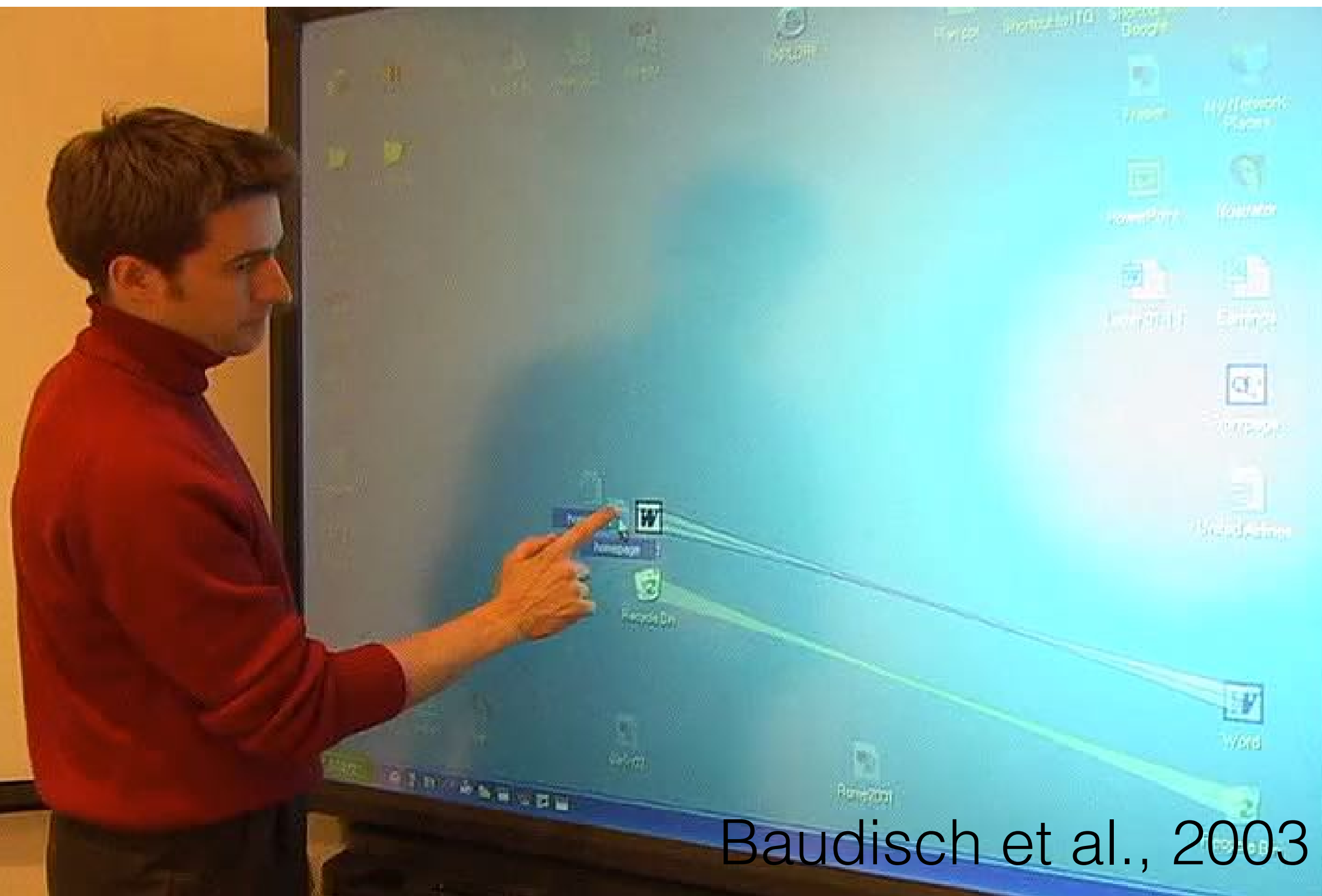


Targets grow
when close to cursor

Pointing time predicted
by expanded target size

But does not work
with dense targets
(example: MacOS dock)

Drag-n-pop



Baudisch et al., 2003

Reducing target distance during drag-and-drop by having target icons “fly” towards the cursor



“Beating” Fitts’ Law

How can the system
help the user
reach the target faster?

1. Extract user intention
2. Use information about targets
3. Breaking the limits

Zoomable user interface (ZUI)

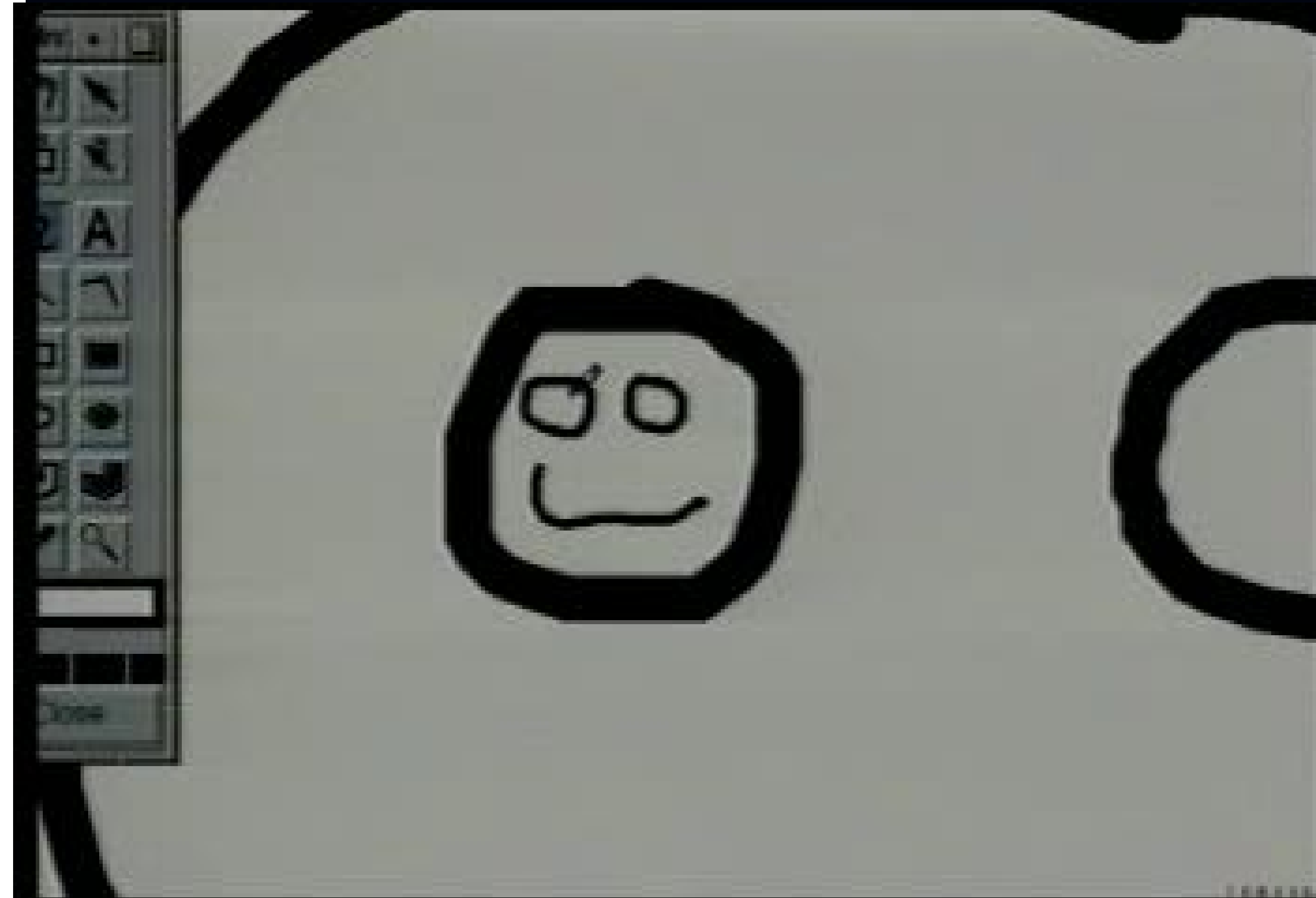
1990	1991	1992	1993	1994
1995	1996	1997	1998	1999

1992			
Jan	Feb	Mar	Apr
May	Jun	Jul	Aug
Sep	Oct	Nov	Dec

1997			
Jan	Feb	Mar	Apr
May	Jun	Jul	Aug
Sep	Oct	Nov	Dec

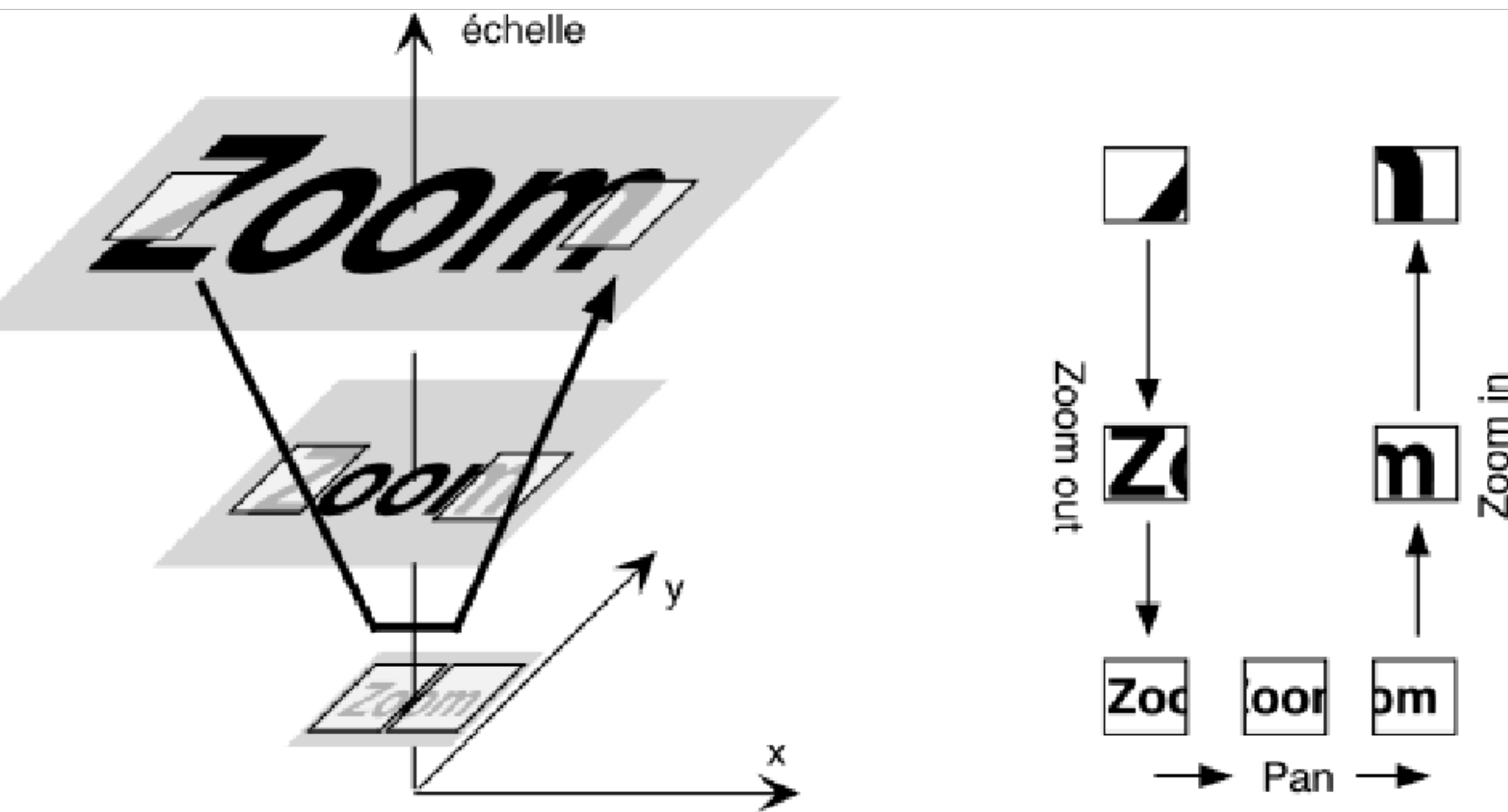
1992	Monday Dec. 7 1992	Tue:
6	7	
1992	Monday Dec. 14 1992	Tue:
3	14	

Perlin & Fox, 1993



Bederson & Hollan, 1994

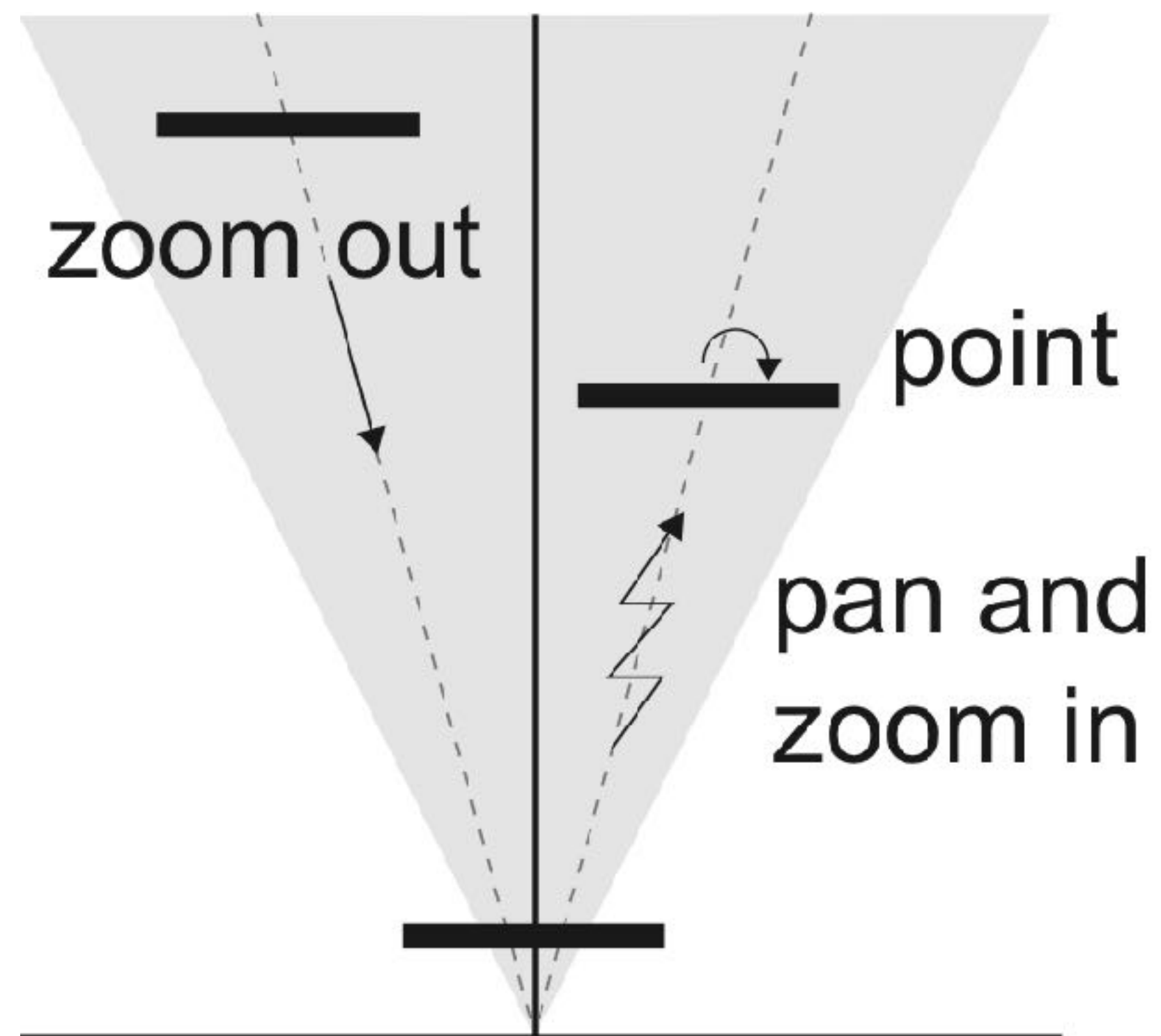
Multiscale pointing



Very different from
“normal” pointing

Zoom out to see the target
Pan and zoom in towards it

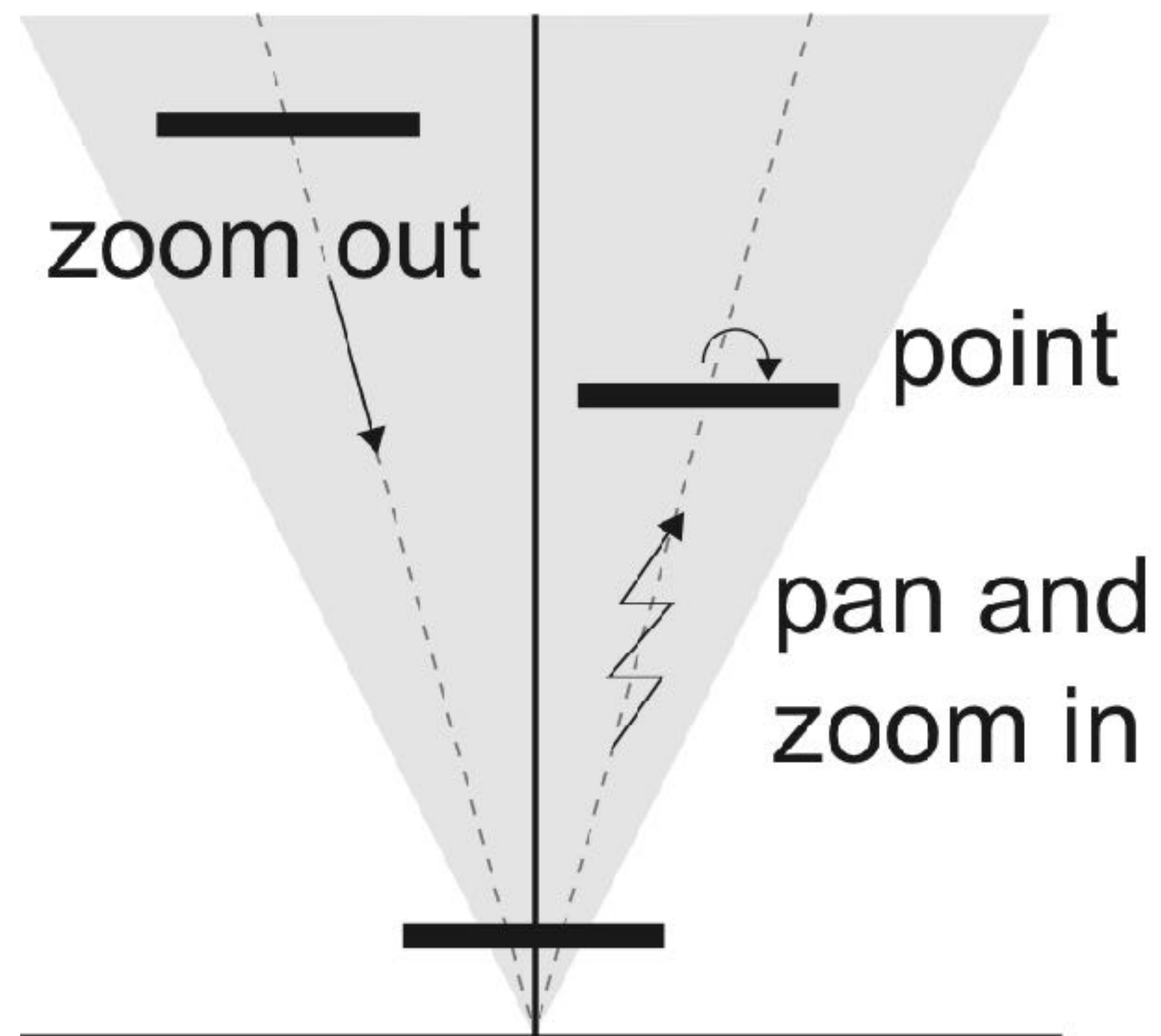
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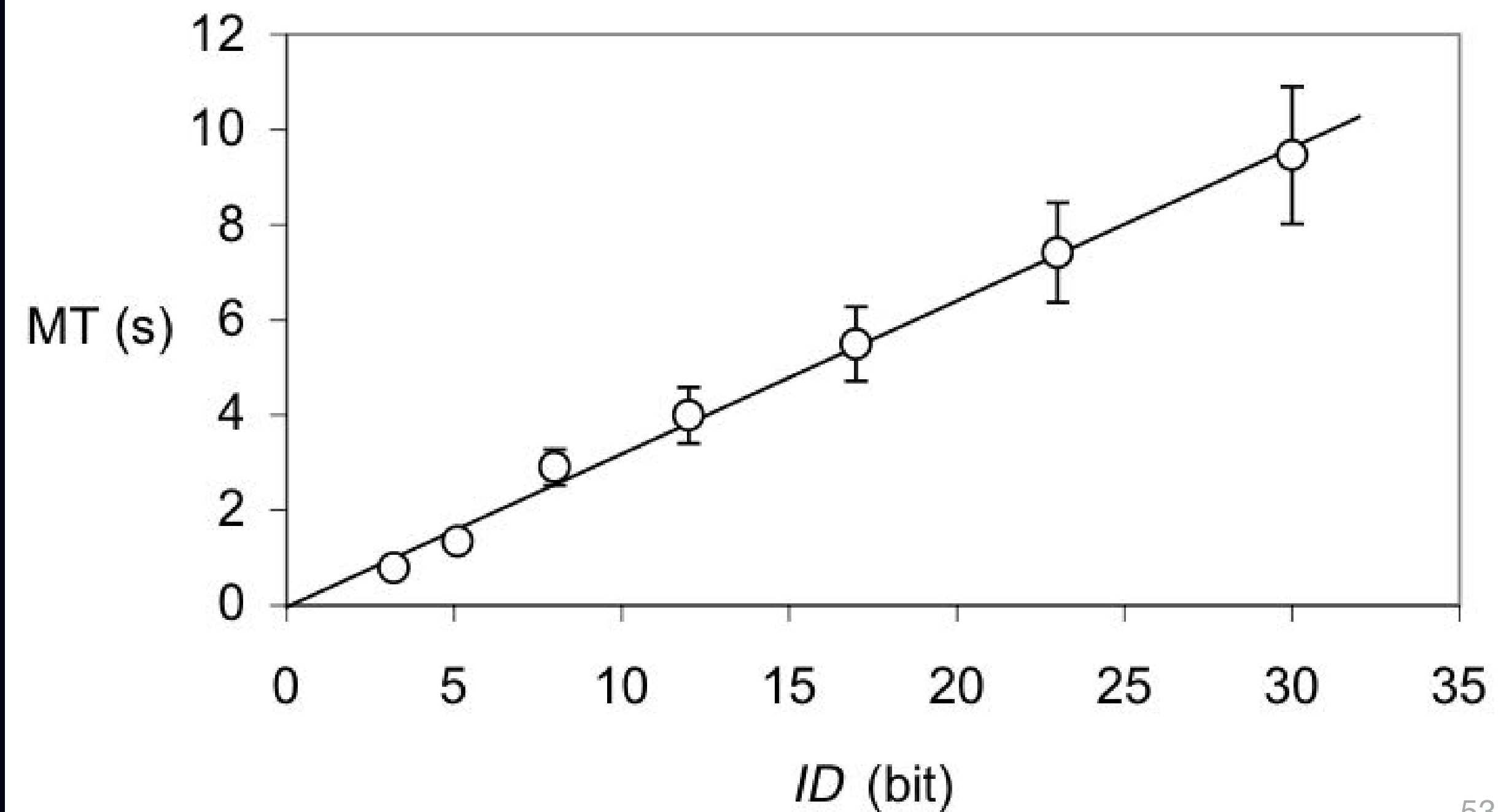
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Multiscale pointing

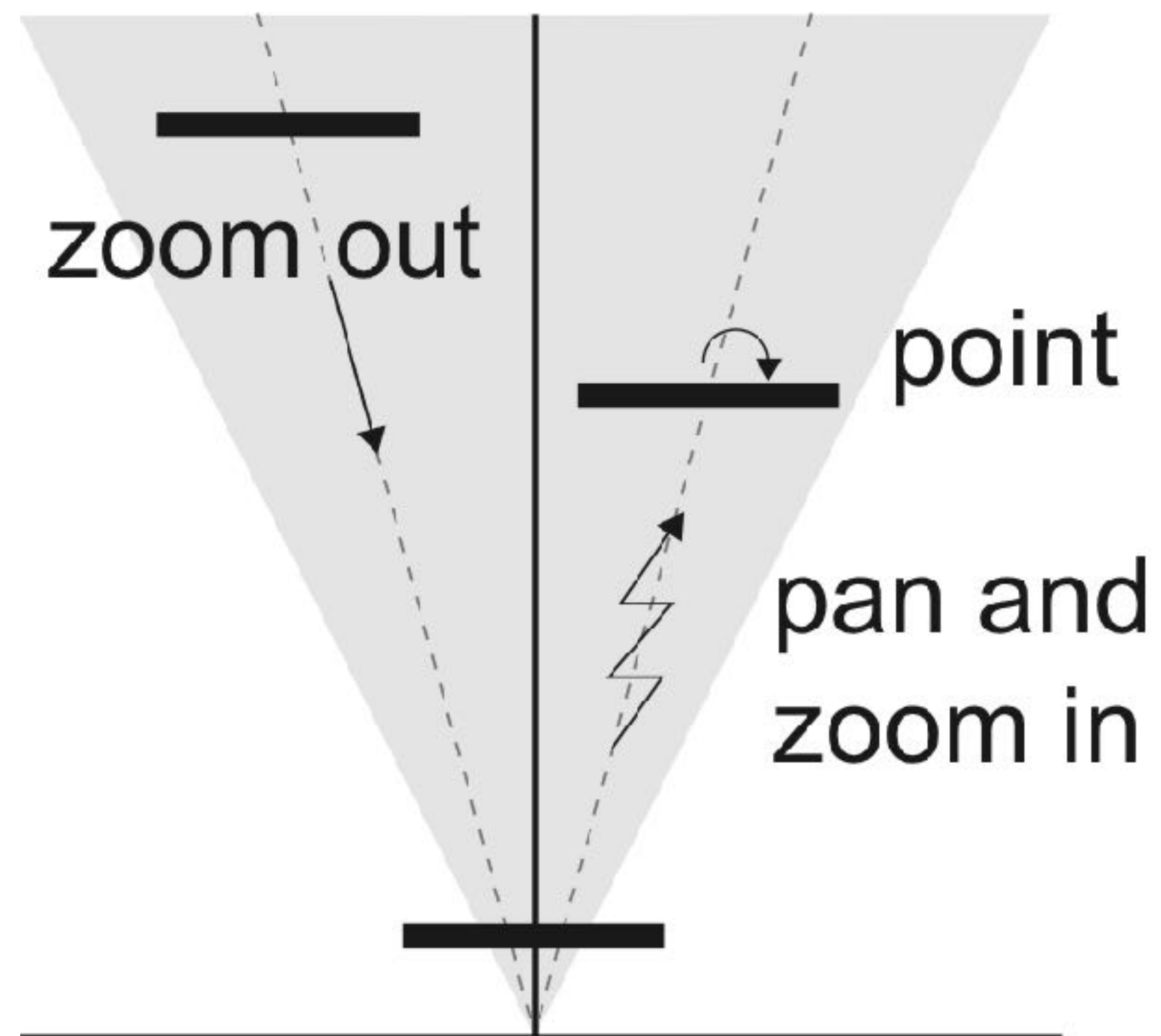


Guiard & Beaudouin-Lafon, 2004

Pointing time predicted
by Fitts' law up to $ID = 30+$



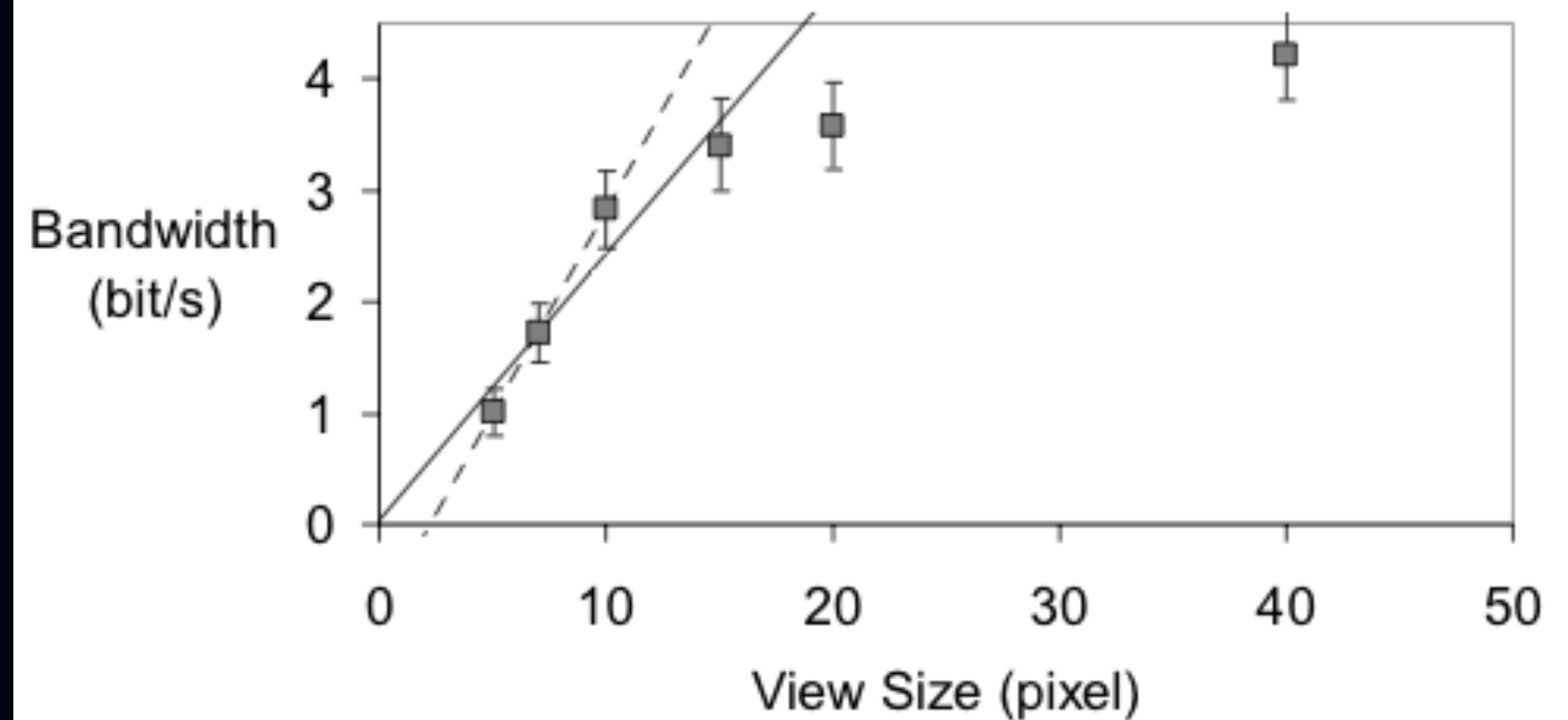
Multiscale pointing



Guiard et al., 2004

Effect of view size

For small views: $MT = k ID / V$



Orthozoom



(a)



(b)

Extend a scrollbar to
pan and zoom a 1D document

Use orthogonal dimension to zoom

Twice as fast
as the best known technique

Orthozoom



(a)



(b)

Appert & Fekete, 2006

The Tragedy of Antony and Cleopatra

Dramatis Personae

MARK ANTONY

OCTAVIUS CAESAR

M. AEMILIUS LEPIDUS

triumvirs.

SEXTUS POMPEIUS

DOMITIUS ENOBARBUS

VENTIDIUS

EROS

SCARUS

DERCETAS

DEMETRIUS

PHILO

friends to Antony.

MECAENAS

AGRIPPA

DOLABELLA

PROCULEIUS

THYREUS

GALLUS

MENAS

friends to Caesar.

MENEKRATES

VARRIUS

friends to Pompey.

TAURUS, lieutenant-general to Caesar.

CANIDIUS, lieutenant-general to Antony.

SILIUS, an officer in Ventidius's army.

EUPHRONIUS, an ambassador from Antony to Caesar.

ALEXAS

MARDIAN, a Eunuch.

SELEUCUS

DIOMEDES

attendants on Cleopatra.

A Soothsayer.

A Clown.

CLEOPATRA, queen of Egypt.

OCTAVIA, sister to Caesar and wife to Antony.

CHARMIAN

IRAS

attendants on Cleopatra.

Officers, Soldiers, Messengers, and other Attendants.

SCENE In several parts of the Roman empire.

ACT I

“Beating” Fitts’ Law

How can the system
help the user
reach the target faster?

1. Extract user intention
2. Use information about targets
3. Breaking the limits
4. Challenge the user

BIG: Bayesian Information Gain

BIG: Bayesian Information Gain

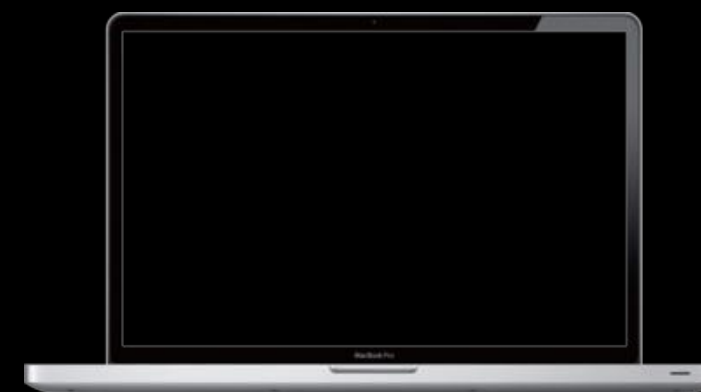
- ❖ **BIG: Bayesian Information Gain**
(Bayesian Experimental Design + Information Theory)



BIG: Bayesian Information Gain

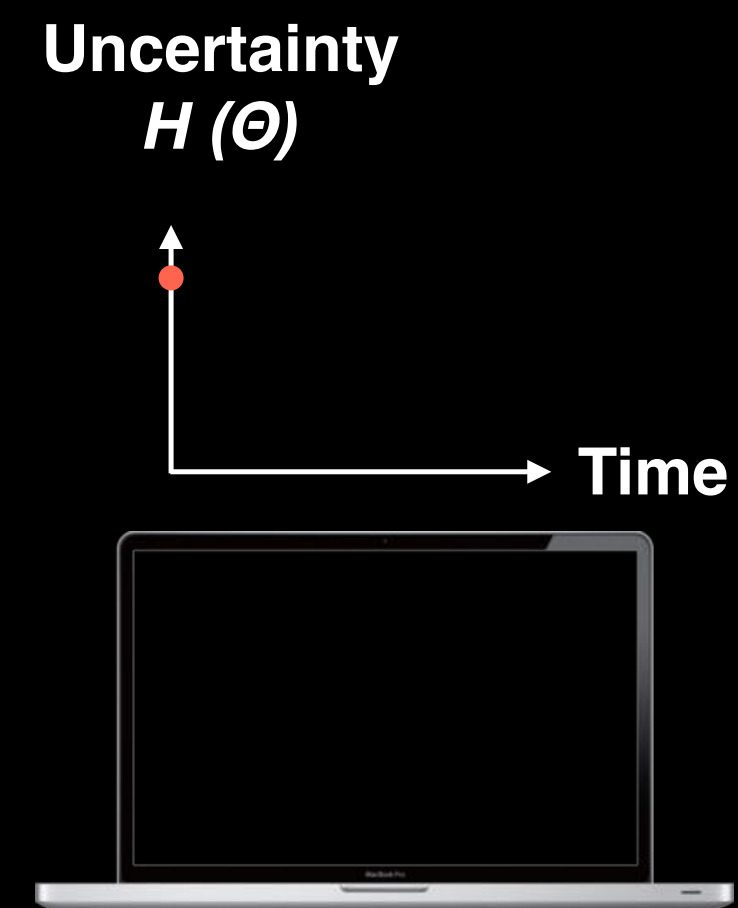
- ❖ **BIG: Bayesian Information Gain**
(Bayesian Experimental Design + Information Theory)

Prior knowledge
 $P(\Theta = \theta)$



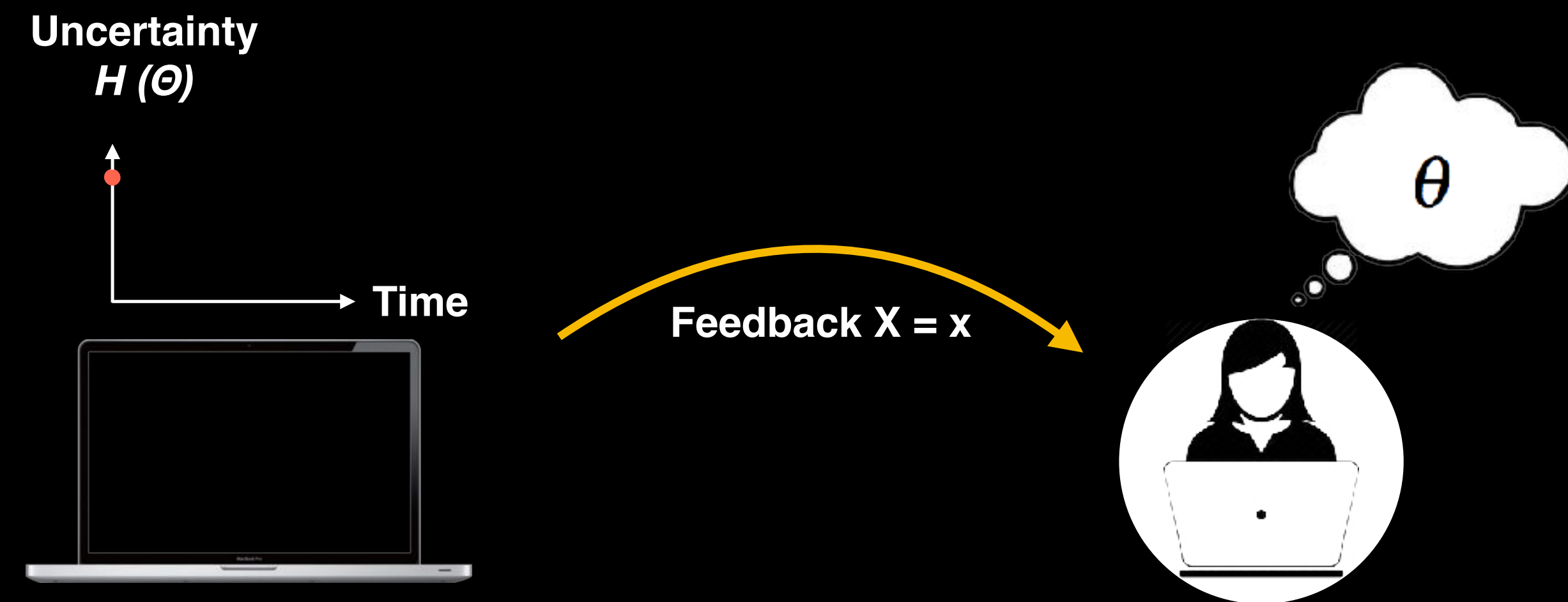
BIG: Bayesian Information Gain

- ❖ **BIG: Bayesian Information Gain**
(Bayesian Experimental Design + Information Theory)



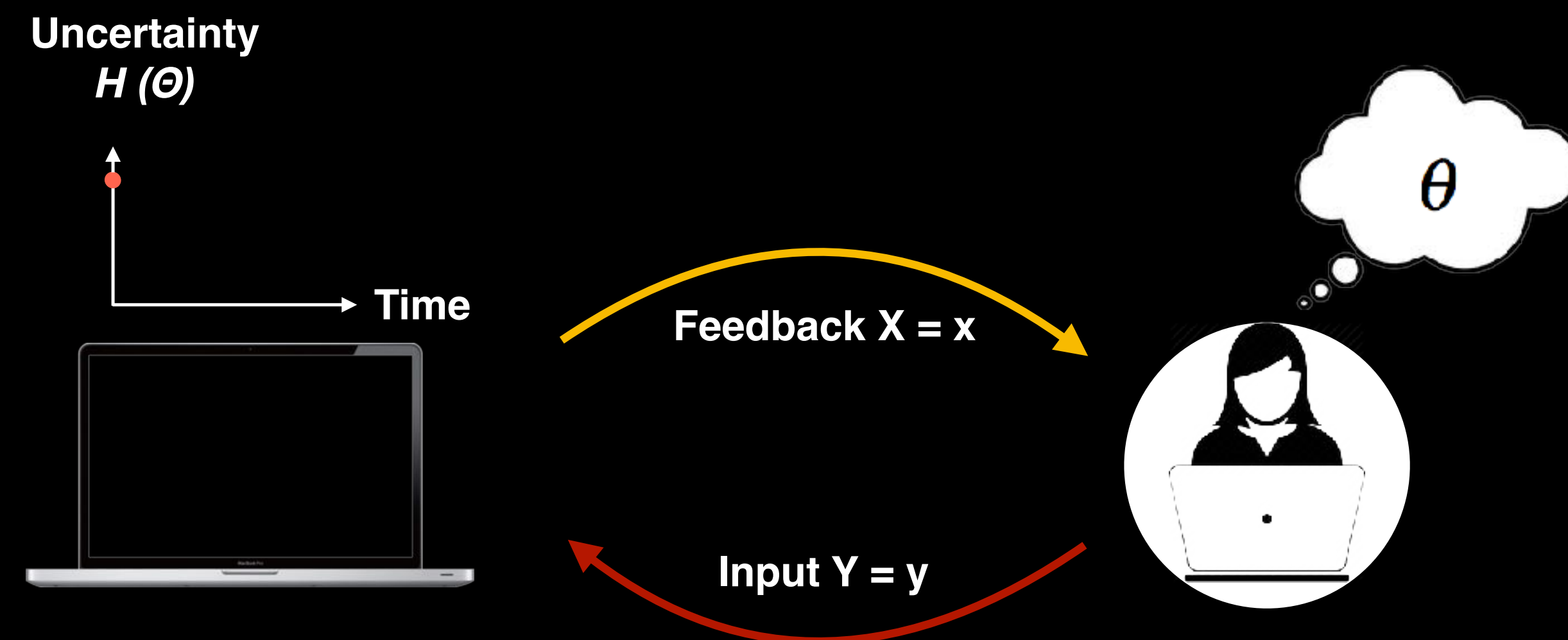
BIG: Bayesian Information Gain

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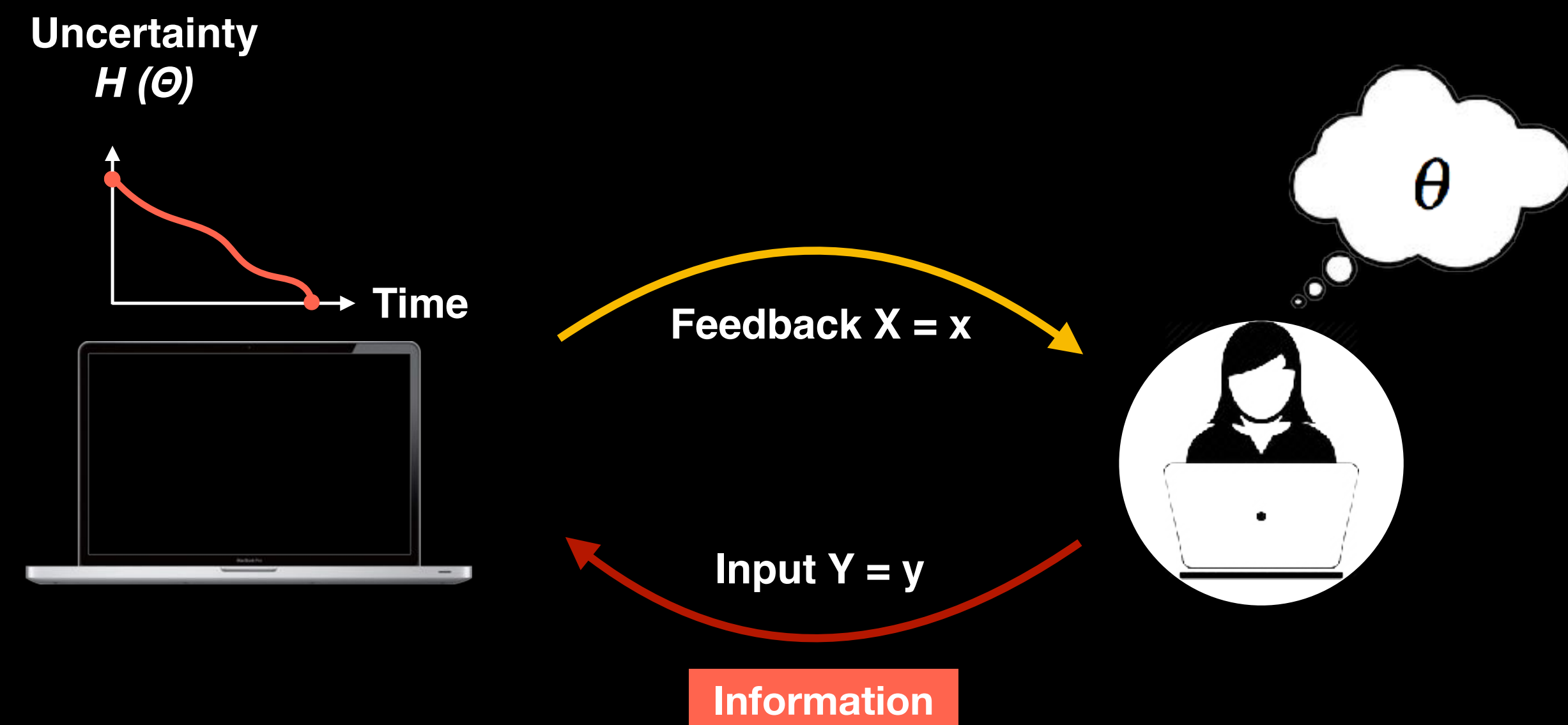
BIG: Bayesian Information Gain

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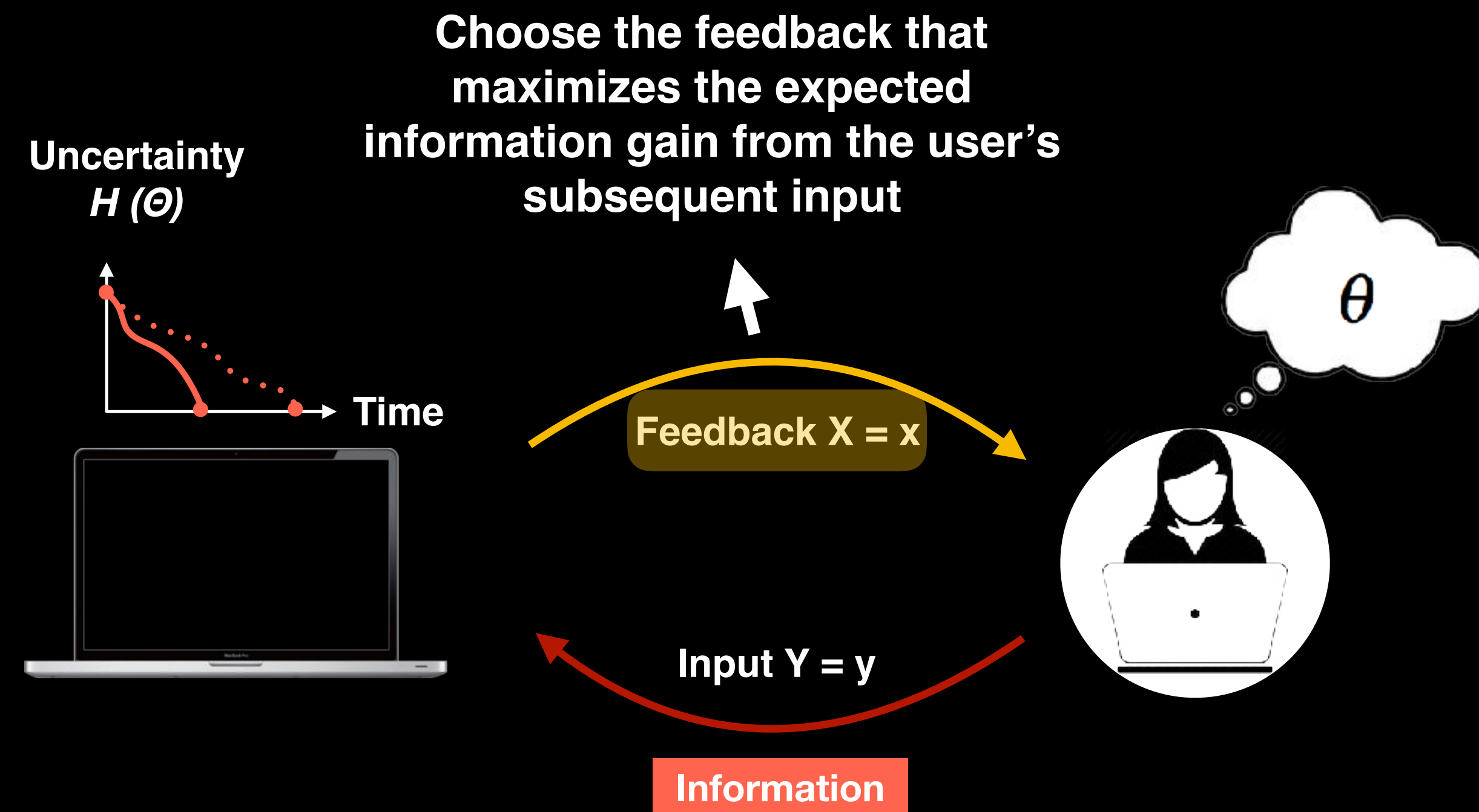
BIG: Bayesian Information Gain

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BIG: Bayesian Information Gain

- ❖ **BIG: Bayesian Information Gain**
(Bayesian Experimental Design + Information Theory)



❖ **BIG: Bayesian Information Gain**

(Bayesian Experimental Design + Information Theory)

- The computer's **Uncertainty** about the user's goal

$$H(\Theta) = -\sum_{i=1}^n P(\Theta = \theta_i) \log_2 P(\Theta = \theta_i)$$

- The computer's **updated knowledge** about the user's goal

$$P(\Theta = \theta | X = x, Y = y) = \frac{P(Y = y | \Theta = \theta, X = x) P(\Theta = \theta)}{P(Y = y | X = x)}$$

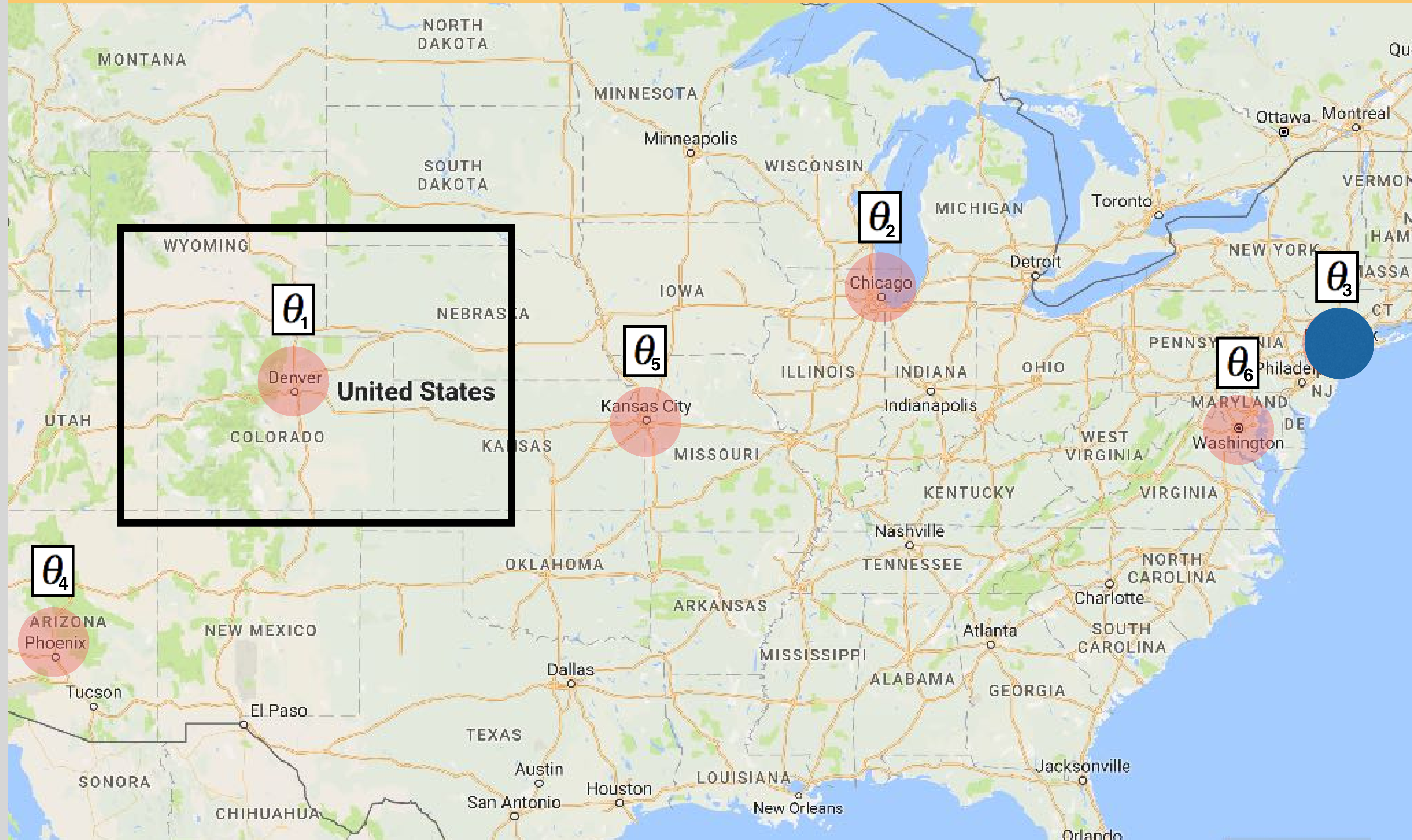
- The **information gained** by the computer from the user's input

$$IG(\Theta | X = x, Y = y) = H(\Theta) - H(\Theta | X = x, Y = y)$$

BIGnav: Bayesian Information Gain Navigation

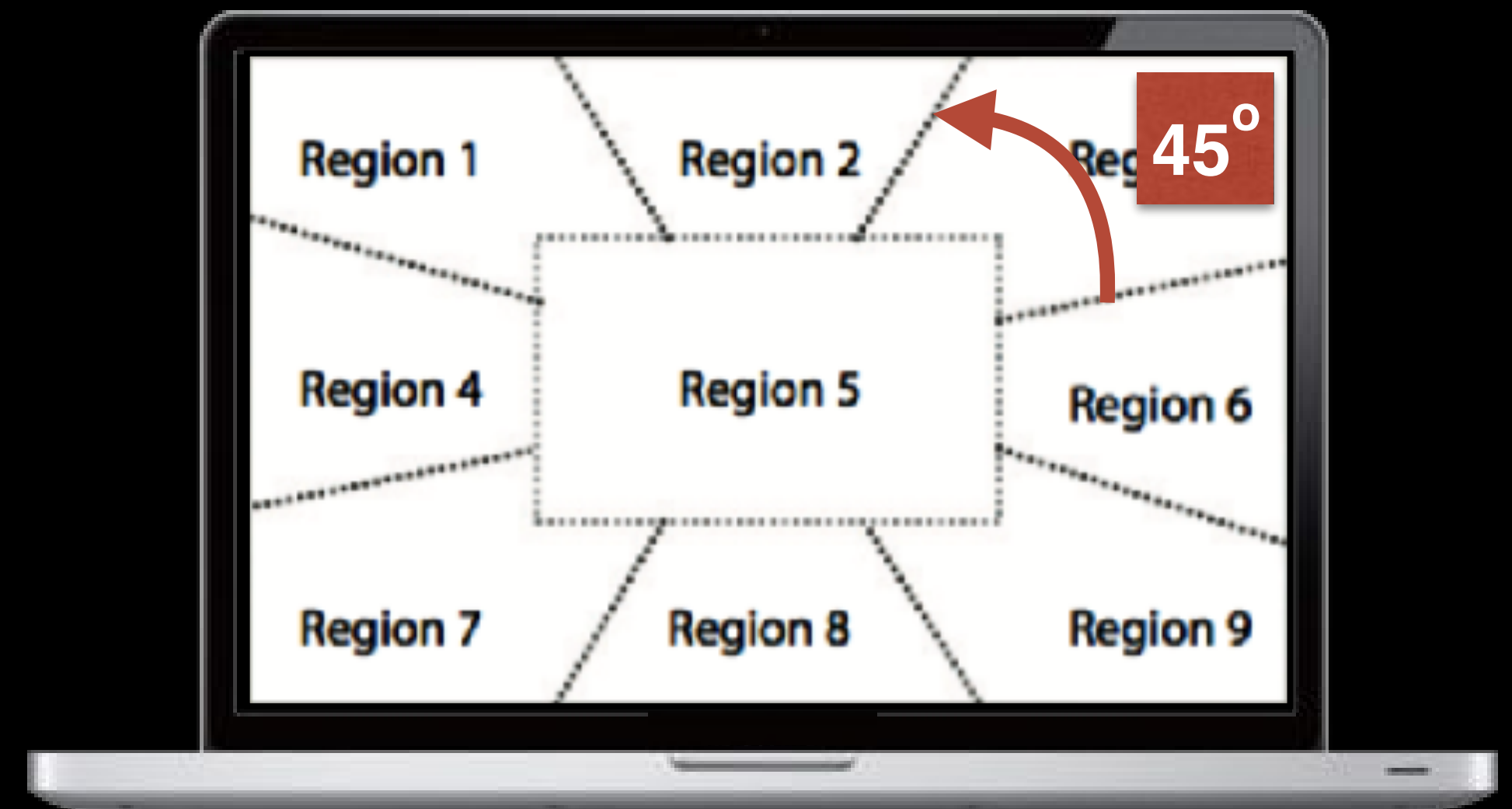


BIGnav: Bayesian Information Gain Navigation

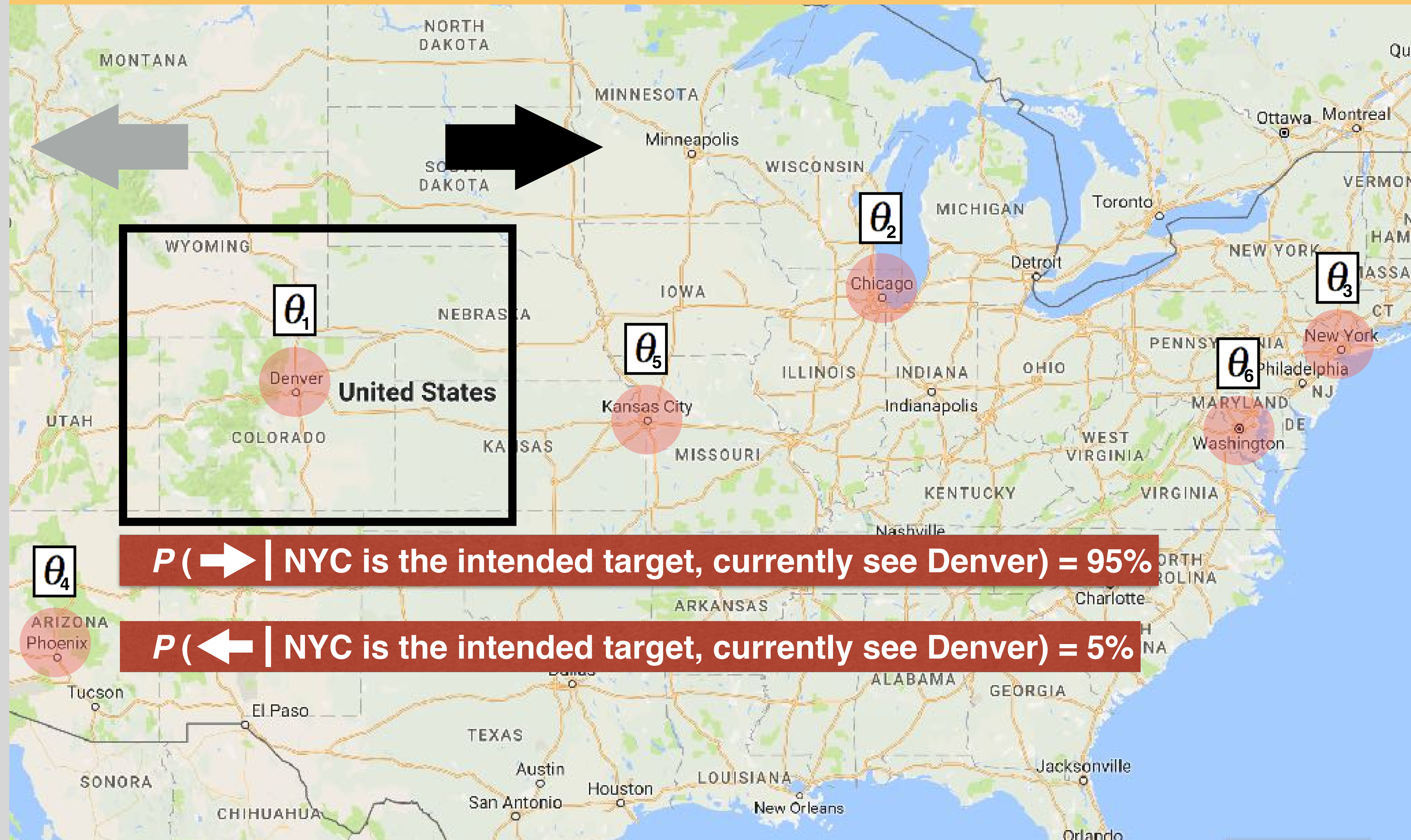


User actions:

8 pan directions
1 zoom-in region



BIGnav: Bayesian Information Gain Navigation



BIGnav: Bayesian Information Gain Navigation

$$P(\Theta = \theta \mid X = x, Y = y)$$

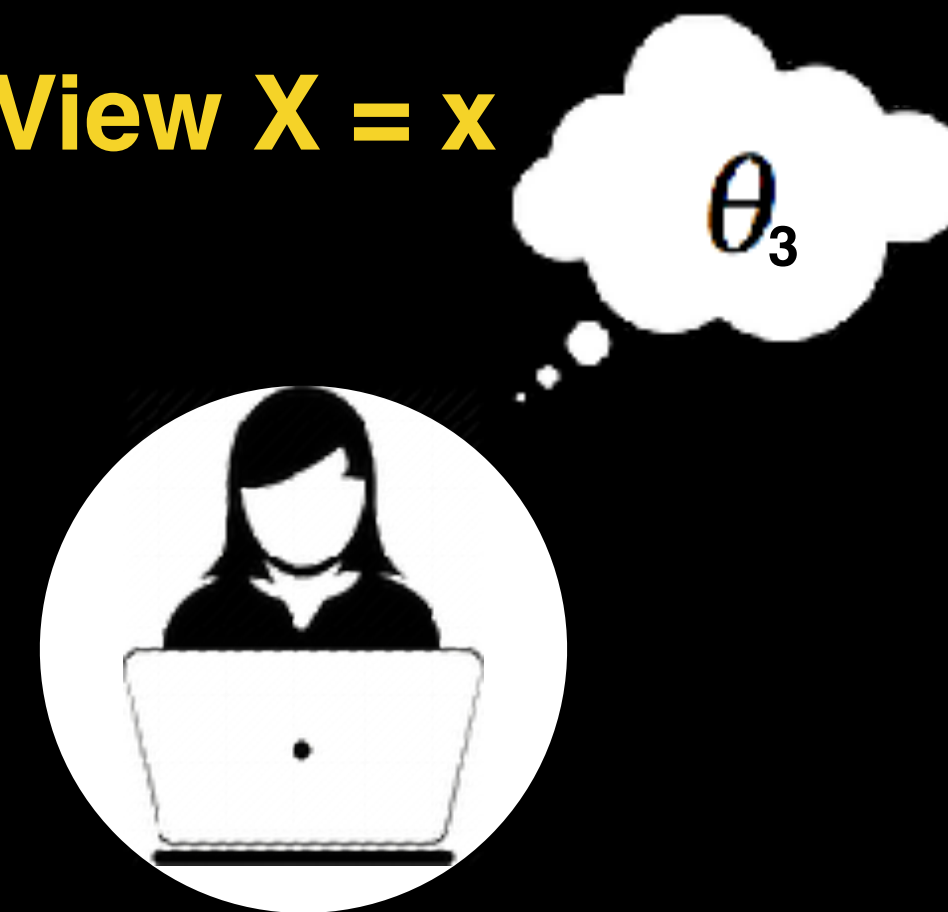
Update its knowledge



$$P(\Theta = \theta_i)$$

User Input $Y = y$

View $X = x$



BIGnav: Bayesian Information Gain Navigation

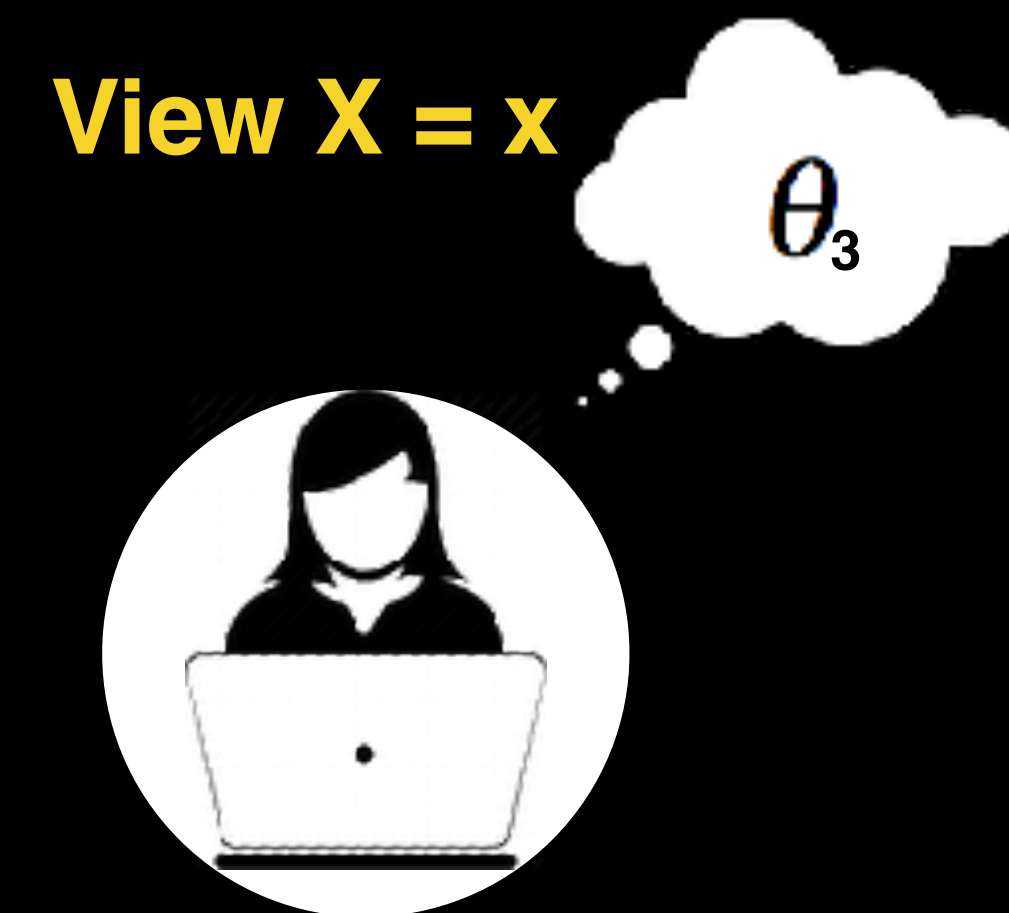
$$IG(\Theta|X = x, Y) = H(\Theta) - H(\Theta|X = x, Y)$$

Navigate to a new view
that maximizes the
expected information gain

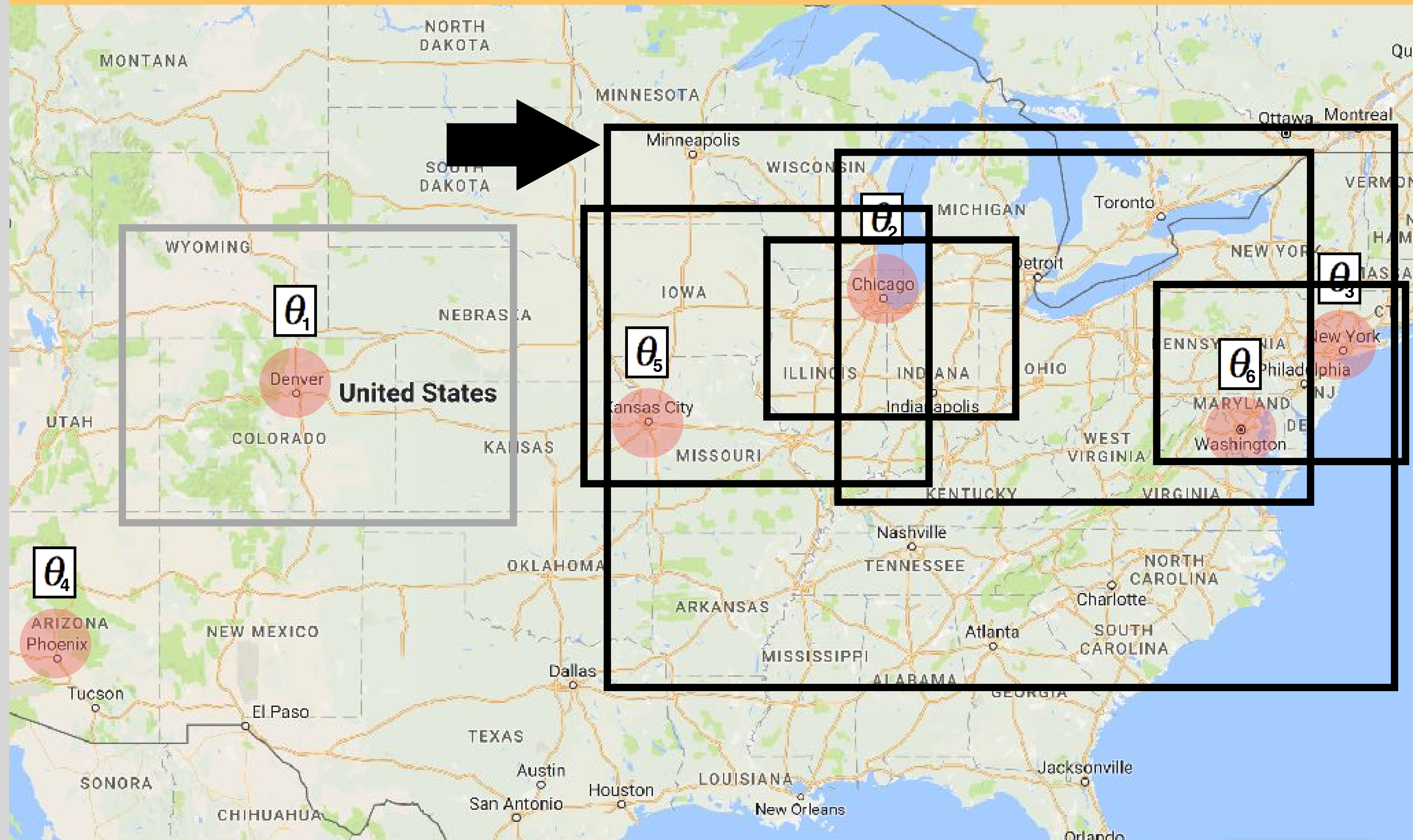


$$P(\Theta = \theta_i)$$

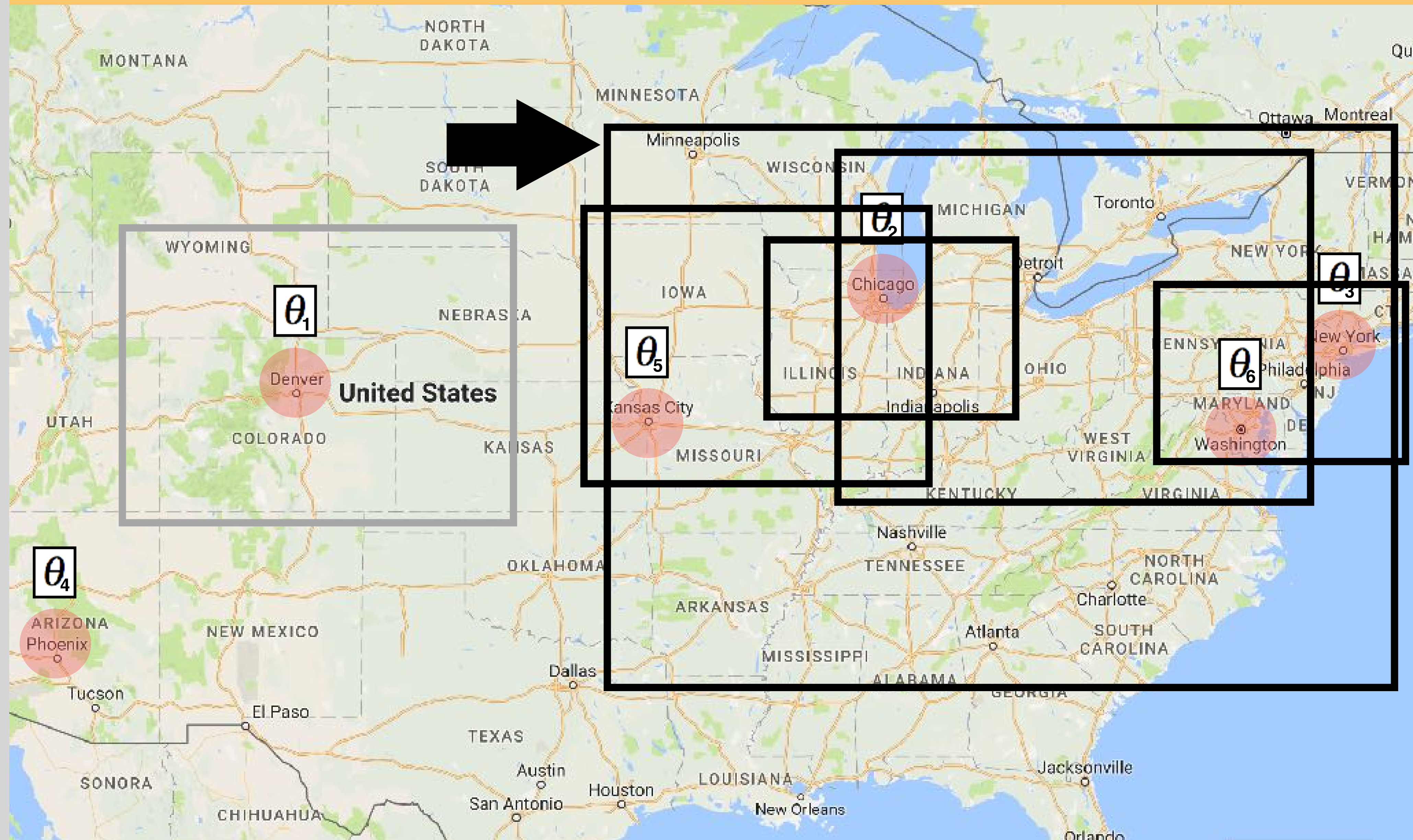
User Input $Y = y$



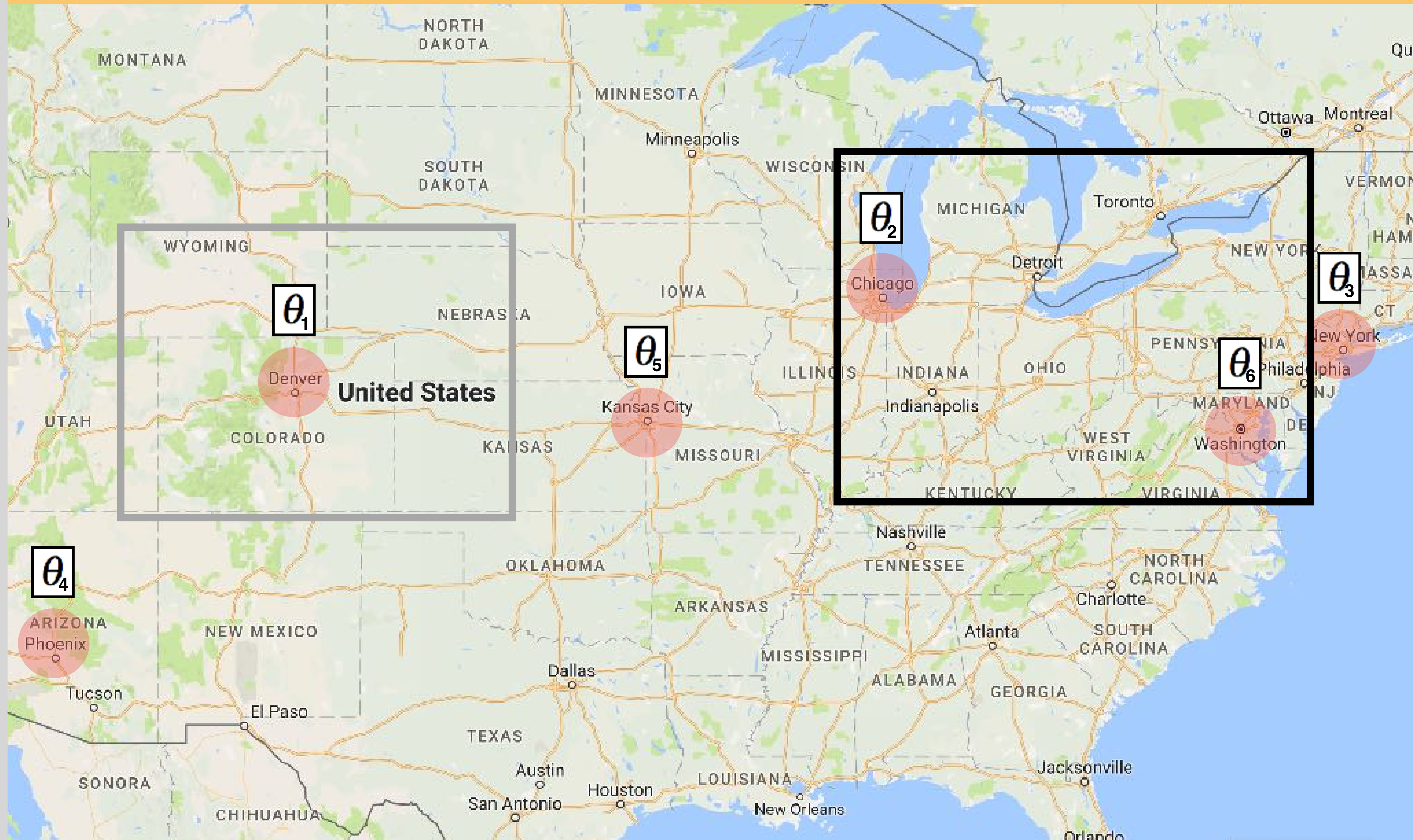
BIGnav: Bayesian Information Gain Navigation



BIGnav: Bayesian Information Gain Navigation



BIGnav: Bayesian Information Gain Navigation



BIGnav: Bayesian Information Gain Navigation

$$IG(\Theta|X = x, Y = y) = H(\Theta) - H(\Theta|X = x, Y = y)$$

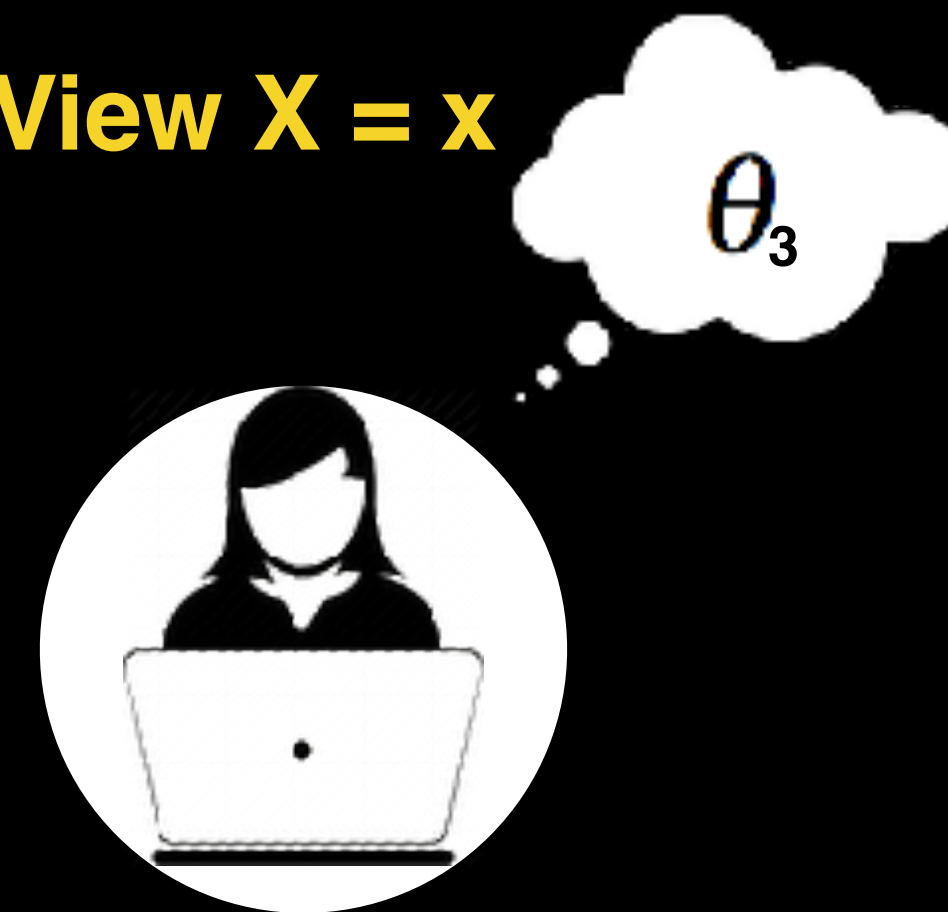
Calculate the actual
information gain



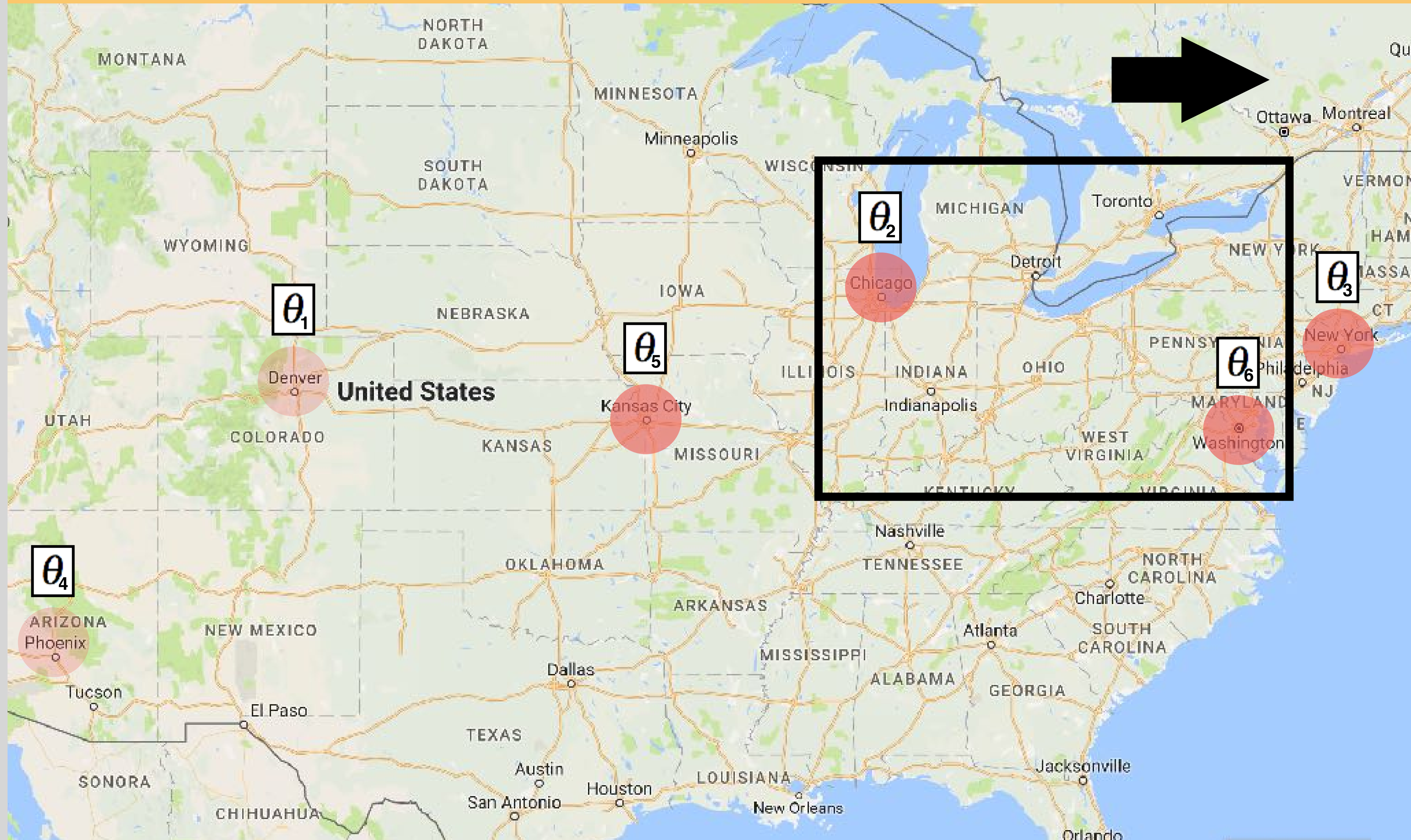
$$P(\Theta = \theta_i)$$

User Input $Y = y$

View $X = x$



BIGnav: Bayesian Information Gain Navigation



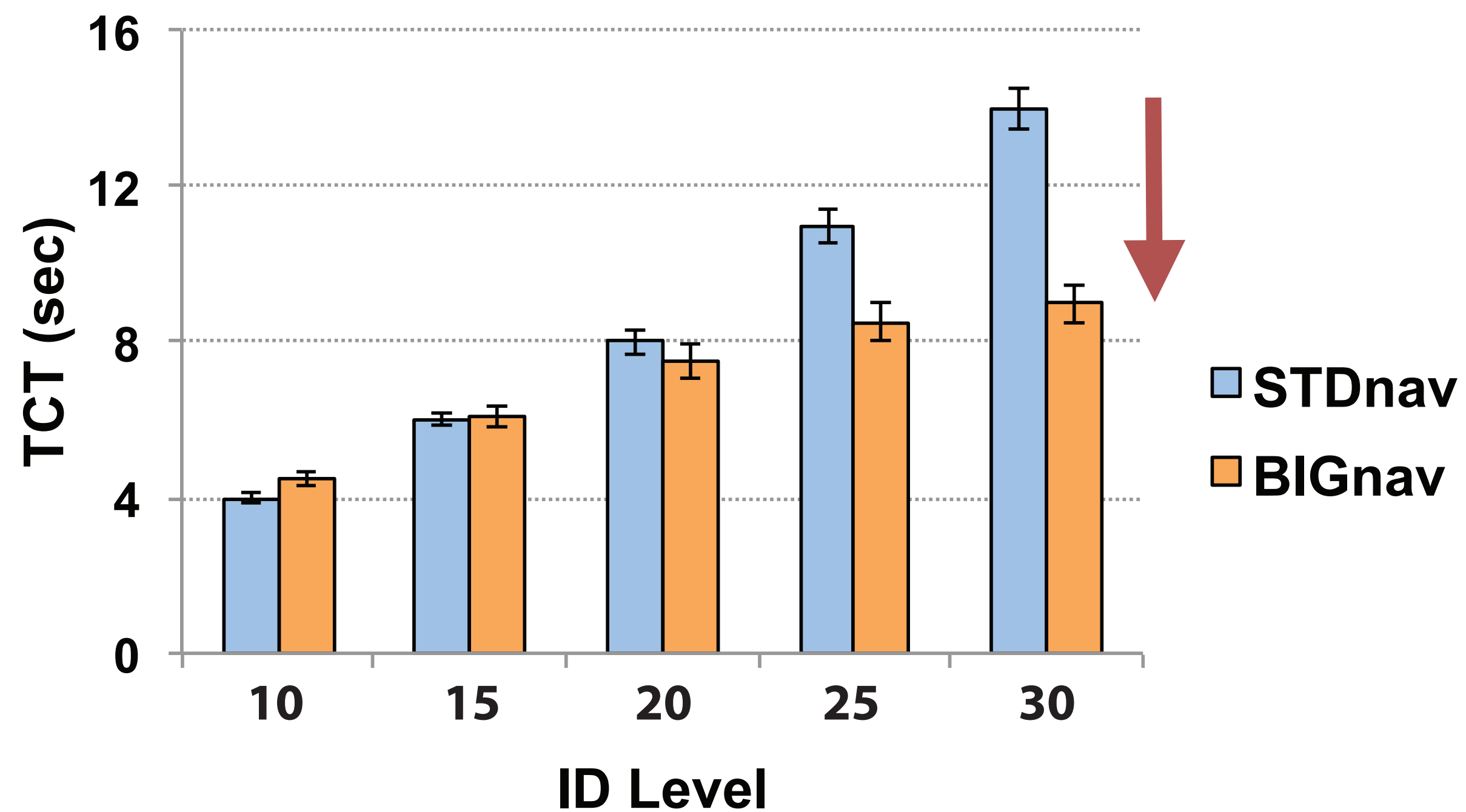


**A map application - “3 steps to go to Paris”.
Europe map featuring large cities with their population as distribution.**



**A map application - “Navigate to Helsinki”.
Europe map featuring large cities with their population as distribution.**

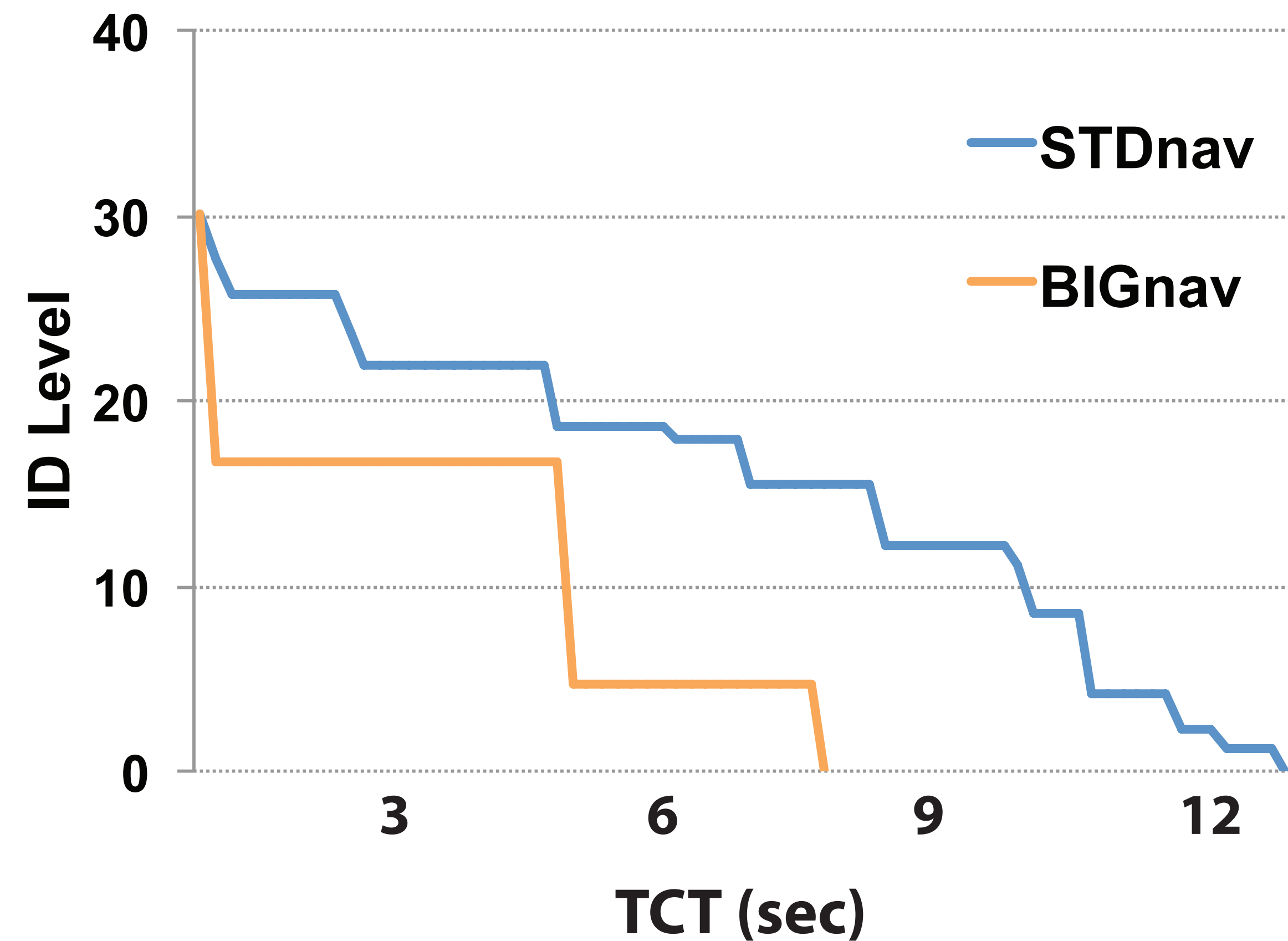
BIGnav



Up to 40% faster than
pan-and-zoom navigation

Higher gain for targets
further away

BIGnav



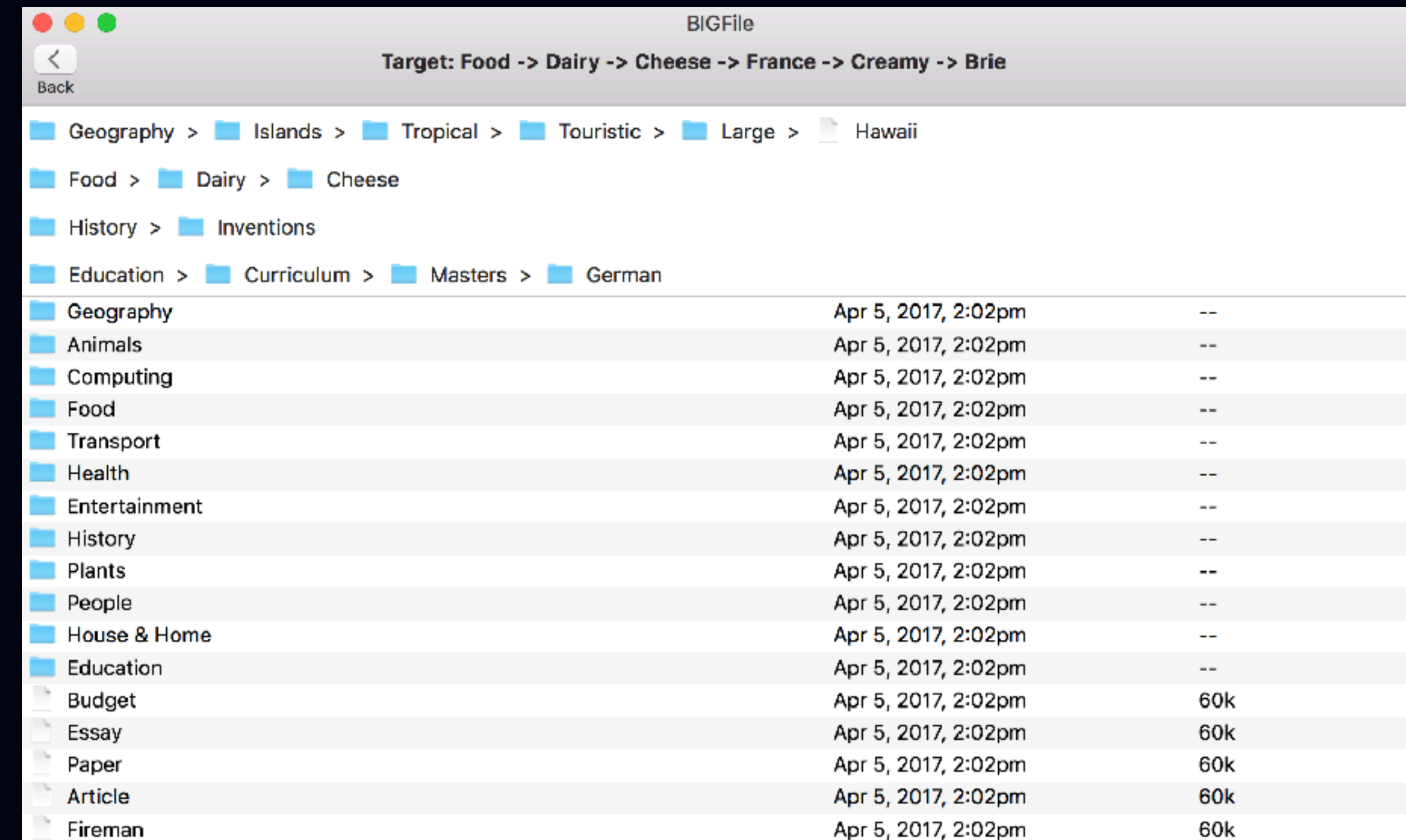
Incurs a high cognitive load

After each move,
long pause before next input

BIG move hard to predict

BIGfile

Same approach
for file retrieval

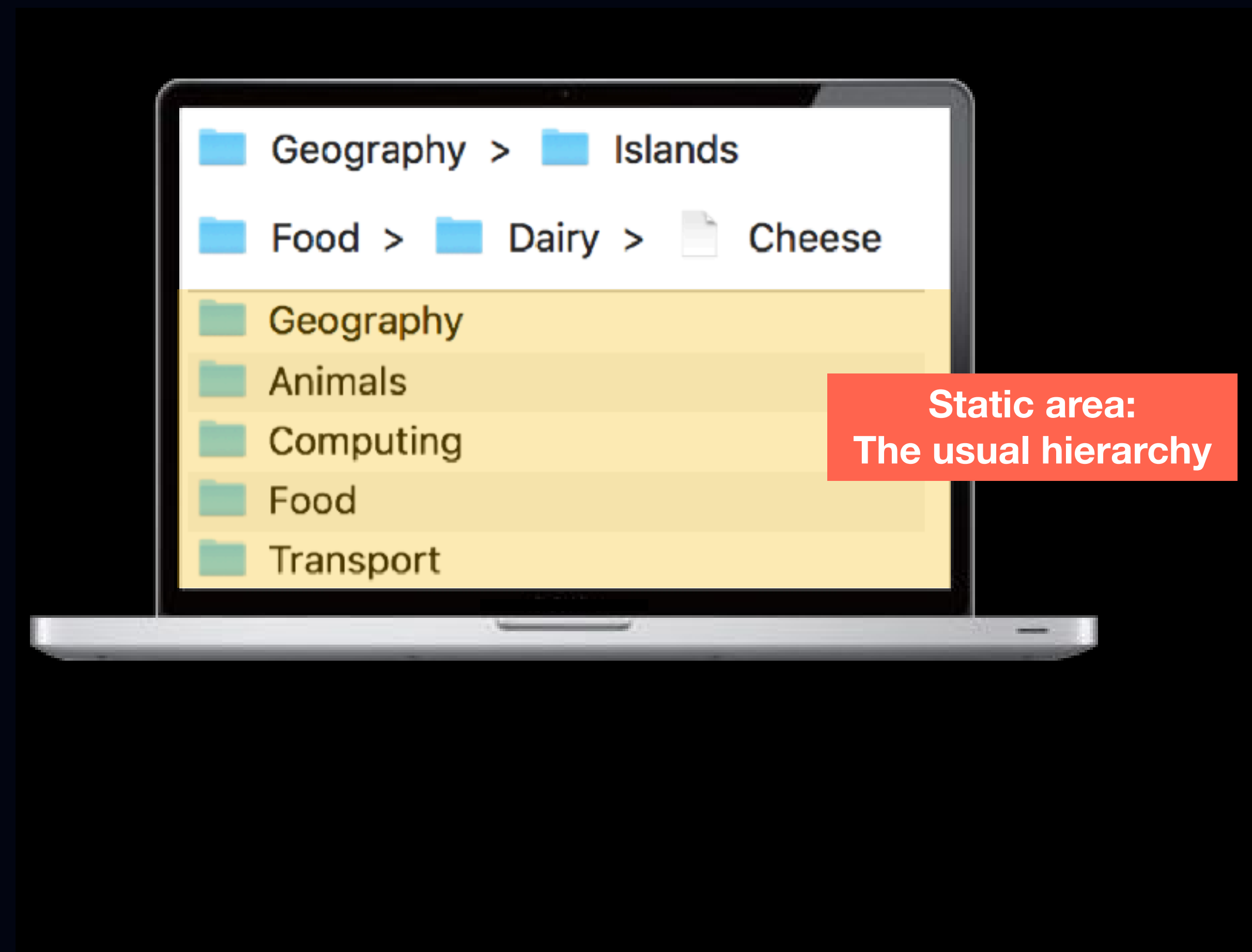


The screenshot shows the BIGFile application window. At the top, the title bar reads "BIGFile". Below it, a navigation bar displays the target path: "Target: Food -> Dairy -> Cheese -> France -> Creamy -> Brie". A "Back" button is located on the left. The main area is divided into two sections. The top section shows a hierarchical tree of folders: Geography > Islands > Tropical > Touristic > Large > Hawaii, Food > Dairy > Cheese, History > Inventions, and Education > Curriculum > Masters > German. The bottom section is a table listing files and folders with their creation dates and sizes.

Geography	Apr 5, 2017, 2:02pm	--
Animals	Apr 5, 2017, 2:02pm	--
Computing	Apr 5, 2017, 2:02pm	--
Food	Apr 5, 2017, 2:02pm	--
Transport	Apr 5, 2017, 2:02pm	--
Health	Apr 5, 2017, 2:02pm	--
Entertainment	Apr 5, 2017, 2:02pm	--
History	Apr 5, 2017, 2:02pm	--
Plants	Apr 5, 2017, 2:02pm	--
People	Apr 5, 2017, 2:02pm	--
House & Home	Apr 5, 2017, 2:02pm	--
Education	Apr 5, 2017, 2:02pm	--
Budget	Apr 5, 2017, 2:02pm	60k
Essay	Apr 5, 2017, 2:02pm	60k
Paper	Apr 5, 2017, 2:02pm	60k
Article	Apr 5, 2017, 2:02pm	60k
Fireman	Apr 5, 2017, 2:02pm	60k

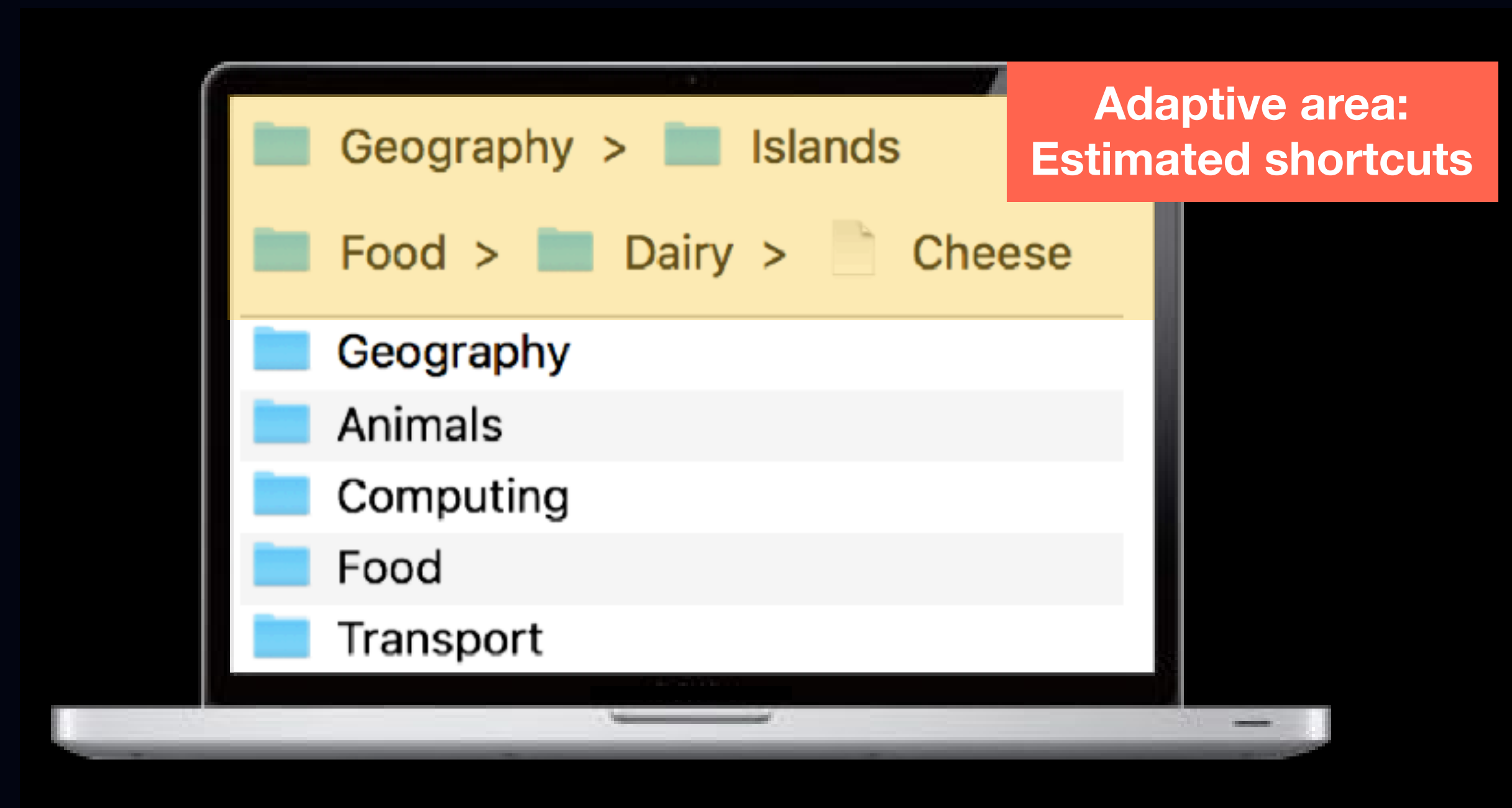
BIGfile

Same approach
for file retrieval



BIGfile

Same approach
for file retrieval



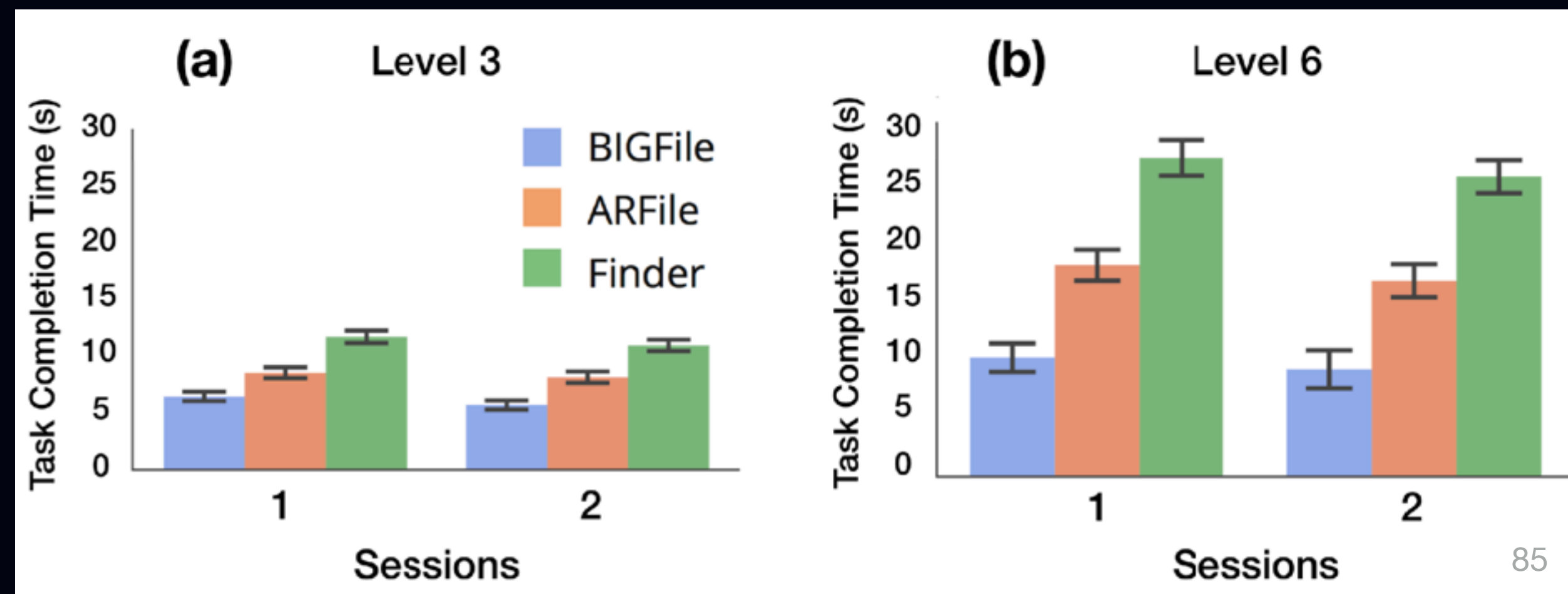
BIGfile

Same approach
for file retrieval

Performance:

44% faster than best technique

64% faster than regular Finder



Conclusion

**Information is a fruitful concept
for interaction**

BUT

**None of these techniques are
available in mainstream interfaces**

**Other possible applications:
text entry, command selection, ...**

Conclusion

Theory-driven HCI leads to generative theories that create novel and powerful techniques

Information theory is a source of inspiration and a tool for future human-computer partnerships



<http://ex-situ.fr>

Merci!

Questions?

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